

Solution for Q.2 (a)

77597

Step 1 - under DC operating conditions

$$V_{TH} = \frac{V_{CC} \cdot R_2}{R_1 + R_2} = \frac{14 \times 30K}{120K + 30K} = 2.8V \longrightarrow \textcircled{1}$$

$$R_{TH} = \frac{R_1 \cdot R_2}{R_1 + R_2} = \frac{120K \cdot 30K}{120K + 30K} = 24K\Omega \longrightarrow \textcircled{2}$$

$$I_B = \frac{V_{TH} - V_{BE}}{R_{TH} + (1 + \beta)R_E} = \frac{2.8 - 0.7}{24K + (101) \times 2.2K} = 8.53 \mu A \longrightarrow \textcircled{3}$$

$$I_E = (1 + \beta) I_B = (1 + 100) \times 8.53 \mu = 0.861 \text{ mA}$$

$$r_e = \frac{26 \text{ mV}}{I_E} = \frac{26 \times 10^{-3}}{0.861 \times 10^{-3}} = 30.198 \Omega \longrightarrow \textcircled{5}$$

Step 2 - under AC operating conditions

Performing AC analysis on the common collector (CC) BJT amplifier we obtain following small signal parameters :-

$$\therefore R_i \text{ or } Z_i = R_1 \parallel R_2 \parallel (1 + \beta)(R_E + r_e)$$

$$\text{Hence } R_i \text{ or } Z_i = 21.68 K\Omega \longrightarrow \textcircled{1}$$

$$\therefore R_o \text{ or } Z_o = R_E \parallel r_e$$

$$\text{Hence } R_o \text{ or } Z_o = 29.78 \Omega \longrightarrow \textcircled{2}$$

$$\therefore A_v = \frac{R_E \parallel R_L}{R_E \parallel R_L + r_e}$$

$$\text{Hence } A_v = 0.9829$$

Step 3 - Lower cut-off frequency (f_L)
 With only two capacitors C_{in} & C_{out} there are only two corner frequencies f_{L1} & f_{L2} present as shown :-

$$\therefore f_{L1} = \frac{1}{2\pi [R_{sig} + R_i] C_{in}} = \frac{1}{2\pi [1k + 21.68k] \times 0.1 \times 10^{-6}}$$

Hence $f_{L1} = 70.174 \text{ Hz}$ (1)

$$\therefore f_{L2} = \frac{1}{2\pi [R_o + R_L] C_{out}} = \frac{1}{2\pi [29.78 + 8.2k] \times 0.1 \times 10^{-6}}$$

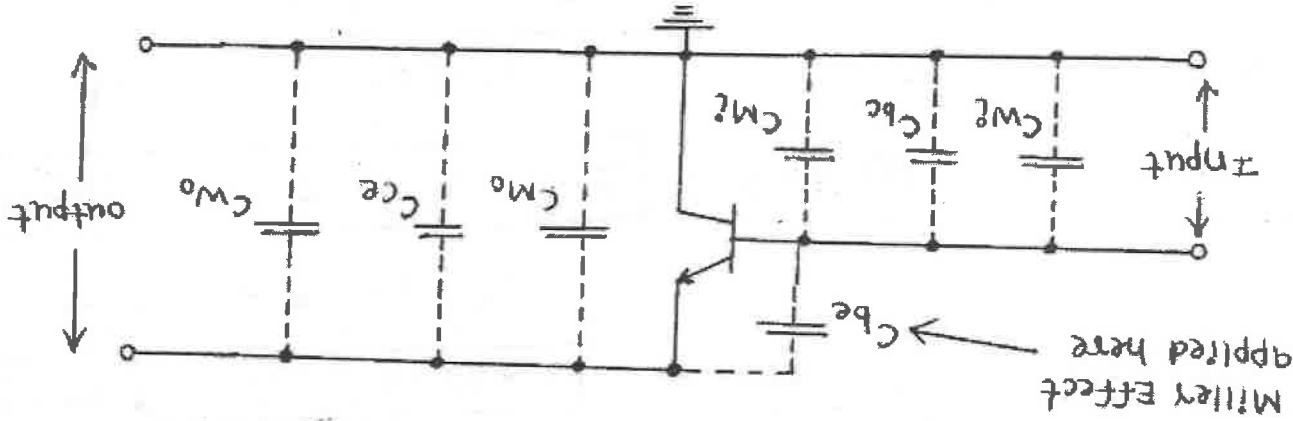
Hence $f_{L2} = 193.38 \text{ Hz}$ (2)

Thus $f_L = \max [f_{L1}, f_{L2}]$ as it is the last corner frequency encountered when the amplifier frequency response moves from lower frequency range to mid-band range.

Hence $f_L = 193.38 \text{ Hz}$

Step 4 - Calculate input & output capacitance (C_i & C_o)

For common collector (CC) BJT configuration the stray/parasitic & wiring capacitances with Miller Effect are as :-



$$C_{M_i} = C_{be} [1 + |A_v|] = [1 + 0.9829] \times 30 \times 10^{-12}$$

Hence $C_{M_i} = 59.487 \text{ pF}$ (1)

$$C_{M_0} = C_{be} \left[\frac{1 + |A_v|}{|A_v|} \right] = \left[1 + \frac{1}{0.9829} \right] \times 30 \times 10^{-12}$$

$$\text{Hence } C_{M_0} = 60.52 \text{ pF} \longrightarrow \textcircled{2}$$

$$\therefore C_i = C_{wi} + C_{bc} + C_{M_i} = 8 \text{ pF} + 20 \text{ pF} + 59.487 \text{ pF}$$

$$\text{Hence } C_i = 87.487 \text{ pF} \longrightarrow \textcircled{3}$$

$$\therefore C_o = C_{wo} + C_{ce} + C_{M_o} = 10 \text{ pF} + 12 \text{ pF} + 60.52 \text{ pF}$$

$$\text{Hence } C_o = 82.52 \text{ pF} \longrightarrow \textcircled{4}$$

Step 5 - Higher cut-off frequency (f_H)

With two capacitances C_i & C_o at input & output side there are two corner frequencies f_{H_1} & f_{H_2} present as shown :-

$$\therefore f_{H_1} = \frac{1}{2\pi [R_{sig} // R_i] C_i} = \frac{1}{2\pi [1\text{K} // 21.68\text{K}] \times 87.487 \times 10^{-12}}$$

$$\text{Hence } f_{H_1} = 1.903 \text{ MHz} \longrightarrow \textcircled{1}$$

$$\therefore f_{H_2} = \frac{1}{2\pi [R_o // R_L] C_o} = \frac{1}{2\pi [29.78 // 8.2\text{K}] \times 82.52 \times 10^{-12}}$$

$$\text{Hence } f_{H_2} = 65.004 \text{ MHz} \longrightarrow \textcircled{2}$$

Always select $f_H = \min[f_{H_1}, f_{H_2}]$ since it is the first high corner frequency encountered by amplifier frequency response before it moves from mid-band range to high frequency.

$$\text{Hence } f_H = 1.903 \text{ MHz}$$

Applying KVL in gate to source loop,

$$-V_{GS} - 2I_{DQ}R_S + V_{SS} = 0 \quad (1)$$

$$V_{GS} = V_{SS} - 2I_{DQ}R_S \quad (2)$$

$$V_{GS} = 12 - 20I_{DQ} \quad (3)$$

For E-MOSFET (N channel), drain current equation (I_{DQ}) is given by

$$I_{DQ} = k_n [V_{GS} - V_{GS(TH)}]^2 \quad (4)$$

where,

$$k_n = \frac{I_{D(on)}}{[V_{GS(on)} - V_{GS(TH)}]^2}$$

$$k_n = 2.6 \text{ mA/V}^2$$

$$I_{DQ} = 2.6 \frac{V_{GS}^2}{V_{GS}}$$

$$\text{Hence, } I_{DQ} = 2.6 \frac{[12 - 20I_{DQ} + 1.5]^2}{12 - 20I_{DQ} + 1.5}$$

$$I_{DQ} = 2.6 \frac{[10.5 - 20I_{DQ}]^2}{10.5 - 20I_{DQ}} \quad (5)$$

$$\therefore I_{DQ} = 2.6 \frac{[400I_{DQ}^2 - 420I_{DQ} + 110.25]}{10.5 - 20I_{DQ}}$$

$$\therefore I_{DQ} = 294.36 - 112.4 I_{DQ} + 1068 I_{DQ}^2 \quad (7)$$

$$\therefore 1068 I_{DQ}^2 - 112.4 I_{DQ} + 294.36 \quad (8)$$

$$I_{DQ1} = 0.54 \text{ mA}, \quad I_{DQ2} = 0.50 \text{ mA}$$

$$V_{GSQ1} = 12 - 20 (0.54 \times 10^{-3}) = 11.91 \text{ V}$$

$$V_{GSQ2} = 2 \text{ V}$$

Since for E-MOSFET (N-channel) V_{GSQ} is greater than threshold voltage of $V_{GS(th)}$ which means only correct value is $+2 \text{ V}$. $\therefore I_{DQ} = 0.5 \text{ mA}$

Applying KVL in drain to source loop,

$$V_{DD} - I_{DQ} R_D - V_{DSQ} - 2 I_{DQ} R_S + V_{SS} = 0 \quad (9)$$

$$\therefore V_{DSQ} = (V_{DD} + V_{SS}) - 2 I_{DQ} R_S - I_{DQ} R_D \quad (10)$$

$$\therefore V_{DSQ} = 24 - I_{DQ} [R_D + 2R_S] \quad (11)$$

$$\therefore V_{DSQ} = 12.35 \text{ V}$$

$$\text{Hence } Q = [12.35 \text{ V}, 0.5 \text{ mA}]$$

$$g_m = 2 \sqrt{k_n I_{DQ}}$$

$$g_m = 2 \sqrt{2.67 \times 0.5} = 2.31 \text{ mS}$$

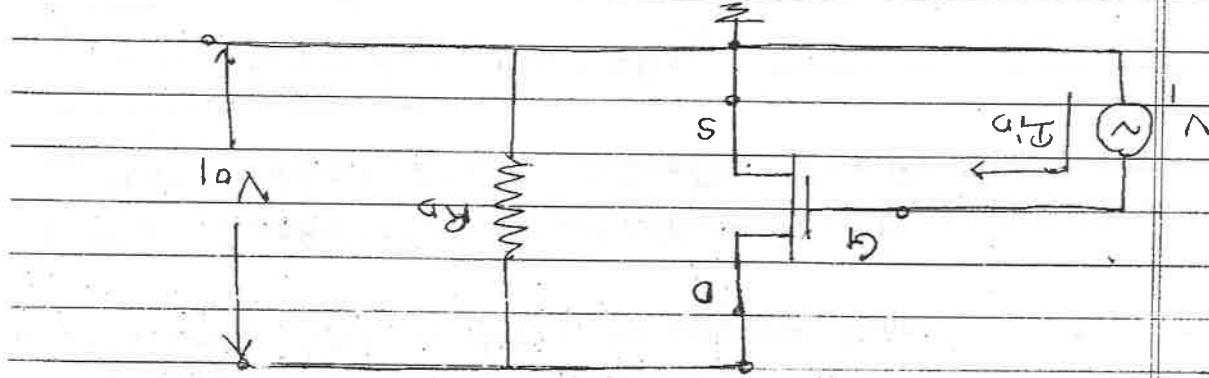
$$g_m = 2.31 \text{ mS}$$

STEP II:- AC operating conditions (AC analysis)

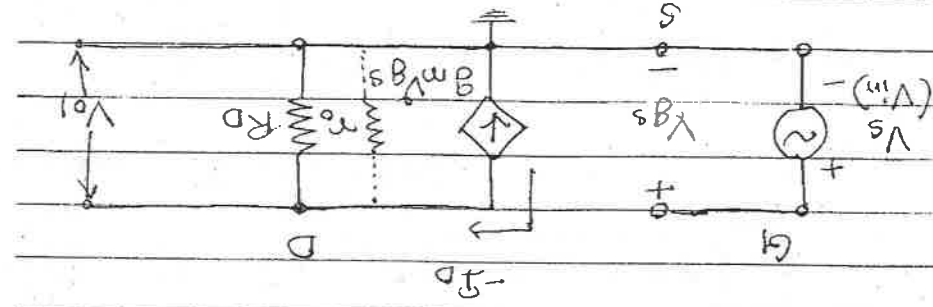
- Remove all DC signal sources ($V_{DD} = -V_{SS} = 0$)
- Short circuit all capacitors if present.

(a) Under differential mode of operation

For differential mode of operation consider $V_1 = -V_2 = V_{in}$ where both i/p signals have same amplitude and frequency but are 180° out of phase with each other due to which emitter resistance is electrically shorted down to ground giving us following equivalent circuit for first stage.



Replace MOSFET by its equivalent mathematical model.



Applying Ohm's law at o/p side,

$$\therefore V_{o1} = -I_D R_D \text{ where } I_D = g_m V_{gs} \quad \text{--- (1)}$$

$$\therefore V_{o1} = -g_m V_{gs} R_D \quad \text{--- (2)}$$

By observation $V_i = V_{gs}$.

$$\therefore \frac{V_{o1}}{V_i} = -g_m R_D \quad \text{--- (3)}$$

Note:- If MOSFET output impedance (small R_D) (r_o) is also present then the AC equivalent circuit contains this value of R_D parallel with externally connected drain resistance R_D giving V_{o1}

$$\frac{V_{o1}}{V_i} = -g_m [R_D \parallel r_o]$$

$$\therefore V_{o1} = -g_m R_D V_i \quad \text{--- (4)}$$

Similarly due to symmetrical configuration;

$$V_{o2} = -g_m R_D V_2 \quad \text{--- (5)}$$

Subtracting $V_{o1} - V_{o2}$,

$$V_{o1} - V_{o2} = -g_m R_D V_1 + g_m R_D V_2$$

$$\therefore V_{o1} - V_{o2} = -g_m R_D [V_1 - V_2] \quad \text{--- (6)}$$

$$V_{o1} - V_{o2} = -g_m R_D (V_1 - V_2)$$

By definition differential mode o/p voltage

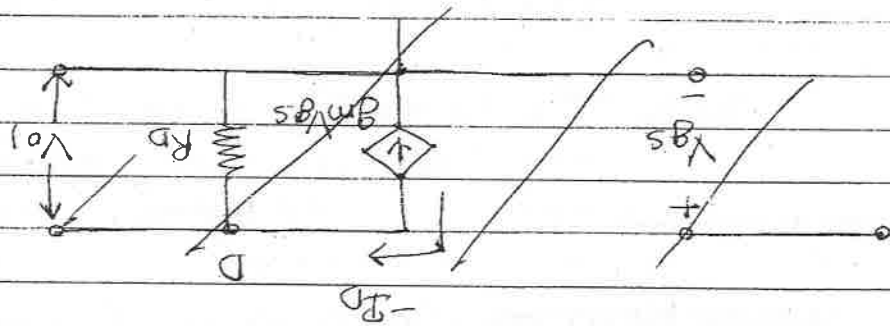
$V_{od} = V_{o1} - V_{o2}$ and differential mode i/p sig
 $V_{id} = V_1 - V_2$ giving differential mode gain

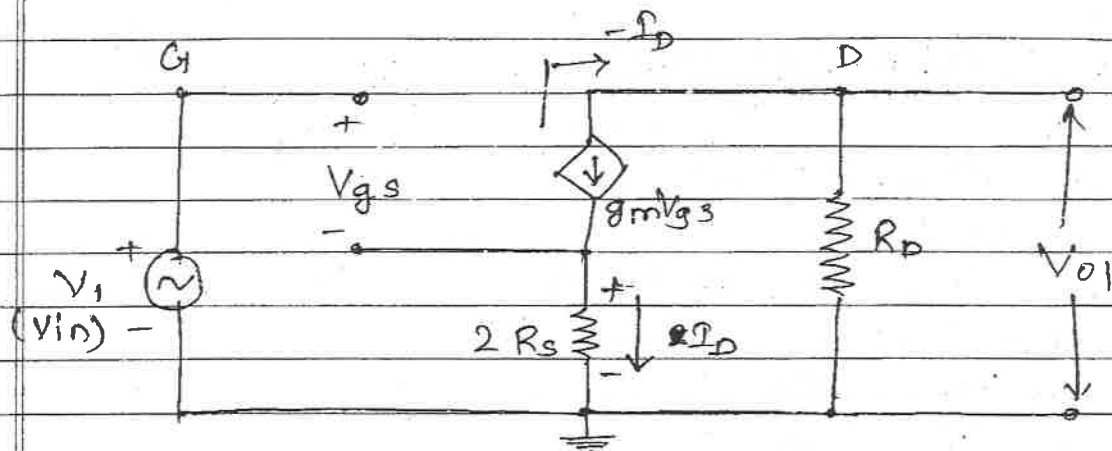
$$A_d = \frac{V_{od}}{V_{id}} = |g_m R_D| = 7.683$$

(b) For common mode of operation

Replace MOSFET by its equivalent mathematical model.

For common mode of operation select $V_1 = V_2 = V$ where both i/p s/g are exactly in phase & o/p same amplitude & frequency thereby making appear as 2R_E for each individual stage giving following AC equivalent circuit for BIT @ 1.





By Ohm's law, at o/p side,

$$V_{o1} = -I_D R_D \quad \text{where } I_D = g_m V_{gs} \quad (1)$$

$$\therefore V_{o1} = -g_m V_{gs} R_D \quad (2)$$

Applying KVL @ the input gate to source loop,

$$V_1 - V_{gs} - 2I_D R_s = 0 \quad (3)$$

where $I_D = g_m V_{gs}$

$$\therefore V_1 = V_{gs} + g_m V_{gs} 2R_s \quad (4)$$

$$\therefore V_1 = V_{gs} [1 + 2g_m R_s] \quad (5)$$

Usually R_s is extremely large hence $2g_m R_s \gg 1$ giving $1 + 2g_m R_s$ approximately equal to $2g_m R_s$.

$$\therefore V_1 = V_{gs} [2g_m R_s]$$

$$\therefore \frac{V_{o1}}{V_1} = \frac{-g_m R_D}{2g_m R_s} = \frac{-R_D}{2R_s}$$

By definition common mode o/p signal V_{oc}

$$V_{oc} = \frac{V_{o1} + V_{o2}}{2} \text{ \& common i/p signal}$$

$$V_{ic} = \frac{V_1 + V_2}{2} \text{ where since } V_1 = V_2 \text{ \& for}$$

$V_{o1} = V_2$, common mode gain is defined as

$$A_c = \frac{V_{oc}}{V_{ic}}$$

$$\therefore A_c = \left| \frac{R_D}{2R_S} \right| = 0.165$$

$$CMRR = \frac{A_D}{A_C} = \frac{g_m R_D}{\frac{R_D}{2R_S}} = g_m R_D \times 2R_S$$

$$= \frac{g_m}{2} = 2g_m R_S$$

$$CMRR = |2g_m R_S|$$

$$CMRR = \frac{7.623}{0.165} = 46.2$$

Solution for Q.4 (b)

Q.1 (a) - Voltage Series Feedback

Calculation of R_{if} :-

Applying KVL in the input loop :-

$$\therefore V_s - V_i - V_f = 0 \longrightarrow \textcircled{1}$$

$$\therefore V_s = V_i + V_f \longrightarrow \textcircled{2}$$

$$\therefore V_s = V_i + \beta_v V_o \longrightarrow \textcircled{3}$$

$$\therefore V_s = V_i + \beta_v A_v V_i \longrightarrow \textcircled{4}$$

$$\therefore V_s = V_i [1 + \beta_v A_v] \longrightarrow \textcircled{5}$$

$$\therefore V_s = I_i R_i [1 + \beta_v A_v] \longrightarrow \textcircled{6}$$

$$\therefore \frac{V_s}{I_i} = R_i [1 + \beta_v A_v] \longrightarrow \textcircled{7}$$

$$\boxed{\text{Hence } R_{if} = R_i [1 + \beta_v A_v]} \longrightarrow \textcircled{8}$$

Calculation of R_{of} :-

Applying KVL in the output loop :-

$$\therefore V_K - I_K R_o - A_v V_i = 0 \longrightarrow \textcircled{1}$$

$$\therefore V_K = I_K R_o + A_v V_i \longrightarrow \textcircled{2}$$

$$\therefore V_K = I_K R_o - A_v V_f \longrightarrow \textcircled{3}$$

$$\therefore V_K = I_K R_o - \beta_v A_v V_K \longrightarrow \textcircled{4}$$

$$\therefore V_K + \beta_v A_v V_K = I_K R_o \longrightarrow \textcircled{5}$$

$$\therefore V_K [1 + \beta_v A_v] = I_K R_o \longrightarrow \textcircled{6}$$

$$\therefore \frac{V_K}{I_K} = \frac{R_o}{1 + \beta_v A_v} \longrightarrow \textcircled{7}$$

$$\boxed{\text{Hence } R_{of} = \frac{R_o}{1 + \beta_v A_v}} \longrightarrow \textcircled{9}$$

Q.1 (b) - 3 stage R-C phase shift oscillator

(i) $R_{TH} = R_1 // R_2 = 68K // 12K = 10.2K\Omega$
 $V_{TH} = V_{CC} \cdot \frac{R_2}{R_1 + R_2} = \frac{12 \times 12K}{12K + 68K} = 1.8V$
 $I_B = \frac{V_{TH} - V_{BE}}{R_{TH} + (1 + \beta)R_E} = \frac{1.8 - 0.7}{10.2K + (1 + 350) \times 1.2K} = 2.55\mu A$
 $I_C = \beta \cdot I_B = 2.55\mu A \times 350 = 0.893mA$
 $V_{CE} = V_{CC} - I_C [R_C + R_E] = 6.7313V$

Hence $Q = [V_{CE}, I_C] = [6.7313V, 0.893mA]$

(ii) $|A_v| = \frac{R_C}{r_e}$ where $r_e = \frac{26mV}{I_E} = 29.03\Omega$

Hence $|A_v| = 161.88$

(iii) $f_0 = \frac{1}{2\pi R_C \sqrt{6+4K}}$ where $K = \frac{R_C}{R}$

Hence $f_0 = 4.821KHz$

(iv) Minimum starting voltage gain required for the sustained oscillations is given by $|A_v| \geq 29$ while the feedback network coefficient is $|B| \leq 1/29$

(v) Ideally each individual/independent R-C network stage provides phase difference of 60° each hence for each individual R-C network we have :-

$$\left\{ \begin{array}{l} \theta_1 = 60^\circ \\ \theta_2 = 120^\circ \\ \theta_3 = 180^\circ \end{array} \right. \quad \theta = \tan^{-1} \left[\frac{R}{X_C} \right] \quad \text{where } X_C = \frac{1}{2\pi fC}$$