

Note

Question one is compulsory

Assume suitable data if necessary

Q1. Solve any four

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- Find out DFT of $X(n) = \{1+5j, 2+6j, -2, -2-2j\}$
- Define normal distribution with equation
- Explain Orthogonal projection component for vector. Compute the orthogonal projection of 'u' on 'a' and vector component of 'u' orthogonal to 'a' of following.

$$u = (-2, 1), a = (9, 2)$$

- Find out Laplace transform of $e^{-3t} \sin^2 t$.
- Show that an isosceles triangle has the smallest perimeter for a given area and a given base.

Q2. A.

A If a continuous random variable X has probability density function

$$f(x) = \begin{cases} e^{-x} & x \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

Find out mean, median, mode and standard deviation.

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Q2.B. Find approximate solution to the using Ritz method

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$$y'' - y + x = 0$$

$$y(0) = 0; y(1) = 0$$

Q3. A. Find out circular cross correlation of following sequence using DITFFT.

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$$x_1(n) = \{1, 2, 3, 4\}$$

$$x_2(n) = \{5, 6, 7, 8\}$$

Q3. B. Given that $\frac{dy}{dx} = 1 + y^2$ where $y(0)$ find $y(0.2)$ using Range kutta fourth order method with $h=0.2$ and $h=0.3$

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Q4. A. Find the least square solution of the linear system $AX=b$ and find orthogonal projection of b on the column space of A . **10**

$$x_1 - x_2 = 4$$

$$3x_1 + 2x_2 = 1$$

$$-2x_1 + 4x_2 = 3$$

Q4.B. If $x_1 = \frac{1}{3}[2 \ -1 \ 2]^T$ and $x_2 = k[3 \ -4 \ 5]^T$ where $k = \frac{1}{50^{1/2}}$. Construct an orthogonal matrix. **10**

Q5.A. Decompose the following matrix using LU decomposition **10**

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix}$$

Q5.A. Use least square method to fit the line $y = a + bx$ based on the sample **10**

$$(2,1), (1/6, -5/6), (-3/2, -2) \text{ and } (-1/3, -2/3)$$

Estimate the total error.

Q6.a. Explain in detail Gauss elimination method. **8**

b. Explain Wavelet Transform in details with application. **10**

c. What is eigen values ? **2**
