

Q.1 (b)

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$$V_g = \text{Pure volume} = \left(\text{vol. of } \overset{\text{Hg}}{\text{helium}} \text{ displaced} \right) - \left(\text{vol. of } \overset{\text{Hel}}{\text{displaced}} \right)$$

$$= 45.1 \text{ cm}^3 -$$

$$= 82.7 - 45.1$$

$$= 37.6 \text{ cm}^3 \text{ per } 101.5 \text{ gm of sample}$$

$$(V_g) = \text{Pure vol per gm of sample} = \frac{37.6 \text{ cm}^3}{101.5 \text{ gm}} = 0.371 \frac{\text{cm}^3}{\text{gm}}$$

The helium volume is also a measure of the density of the solid material in the catalyst

$$\rho_s = \frac{\text{wt. of cat (sample)}}{\text{vol. of helium displaced}} = \frac{101.5 \text{ gm}}{45.1 \text{ cm}^3}$$

$$\rho_s = 2.25 \text{ gm/cm}^3$$

we know that porosity or void fraction, $\epsilon_p = \frac{V_g \rho_s}{V_g \rho_s + 1}$

$$\therefore \epsilon_p = \frac{0.371 \times (2.25)}{0.371 \times (2.25) + 1} = 0.455$$

$$\boxed{\epsilon_p = 0.455} \quad (45.5\% \text{ of porosity})$$

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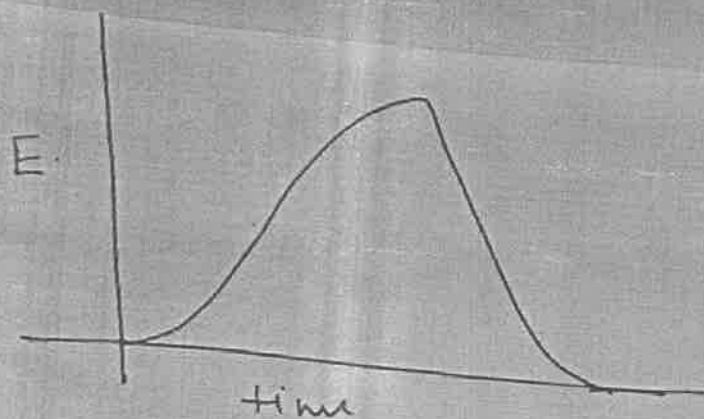
→ $\int_0^{14} C dt = 47.4 \text{ (g min)/m}^3$

$E = \frac{C}{\int_0^{\infty} C \cdot dt}$

t	0	1	2	3	4	5	6	7	8	9	10	12	14
C	0	1	5	8	10	8	6	4	3	2.2	1.5	0.60	0
E	0	0.02	0.10	0.16	0.2	0.16	0.12	0.08	0.06	0.04	0.03	0.012	0

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$$\int_{7.75}^{8.25} E \cdot dt = 0.03 \quad (3\%)$$

$\therefore$ 3% of the fluid leaving the vessel has been in the vessel between 7.75 & 8.25 min

$$\int_3^6 E \cdot dt = 0.195 \quad (19.5\%)$$

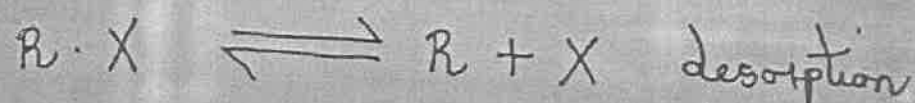
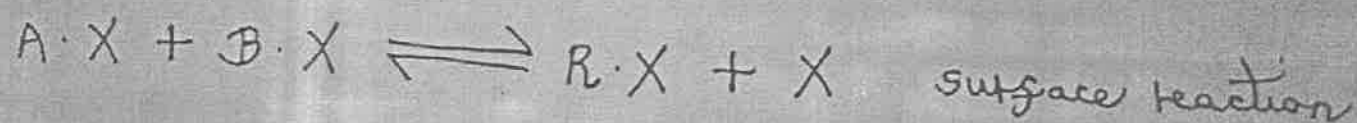
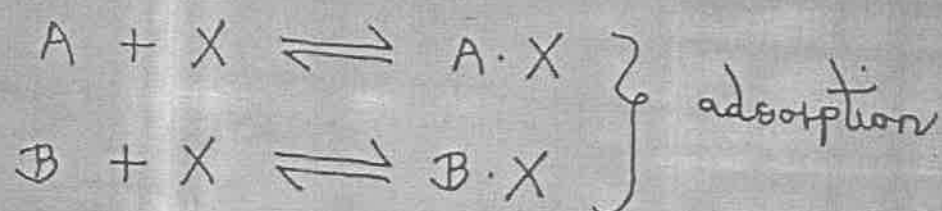
i.e. 19.5% of the material leaving the vessel has spent 3 min or less in the vessel.

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Page-4 Q. 3 (a)

Solution:

The given gas-solid catalytic reaction system may be represented as follows:



Page - 5 Q.3 (a)

If adsorption of B is the rate limiting step, then the adsorption of A, the surface reaction, and the desorption of R will occur at equilibrium.

The rate can be formulated from the adsorption equation which is

$$r_b = k_b \left(C_B \bar{C}_v - \frac{1}{K_B} \bar{C}_B \right) \quad (\text{Equation 1})$$

The adsorbed concentration $\bar{C}_B$ in this expression is obtained from the equilibrium equations for the surface rate, adsorption of A and desorption of R which are as follows:

$$K_B = \left(\frac{\bar{C}_v \bar{C}_R}{\bar{C}_A \bar{C}_B} \right)_{eq} \quad (\text{Equation 2})$$

$$(\bar{C}_A)_{eq} = K_A C_A \bar{C}_v \quad (\text{Equation 3})$$

$$(\bar{C}_R)_{eq} = K_R C_R \bar{C}_v \quad (\text{Equation 4})$$

$$\text{Hence, } \bar{C}_B = \frac{\bar{C}_v \bar{C}_R}{K_B \bar{C}_A} = \frac{\bar{C}_v (K_R C_R \bar{C}_v)}{K_B (K_A C_A \bar{C}_v)} = \frac{\bar{C}_v K_R C_R}{K_B K_A C_A}$$

Page - 5 Q.3 (a)

in the relationship of the several equilibrium constants,

$$K = \frac{K_A K_B}{K_R} \cdot K_S \quad \text{or} \quad \frac{K_R}{K_S K_A} = \frac{K_B}{K} \quad (\text{Equation 6})$$

The expression for $\bar{C}_B$ may be simplified to

(Equation 7)

$$\bar{C}_B = \frac{K_B \bar{C}_V C_R}{K C_A}$$

Substituting this value of $\bar{C}_B$ in the rate-controlling equation (Equation 1) gives:

$$r_b = r = k_b \left(\bar{C}_B \bar{C}_V - \frac{1}{K_B} \cdot \frac{K_B \bar{C}_V C_R}{K C_A} \right)$$

(Equation 8)

$$\therefore r_b = k_b \bar{C}_V \left(\bar{C}_B - \frac{1}{K} \cdot \frac{C_R}{C_A} \right)$$

The expression for $\bar{C}_V$ can be formulated as follows:

The concentration of vacant sites can be expressed in terms of the total concentration of sites $\bar{C}_M$,

(Equation 9)

$$\bar{C}_M = \bar{C}_V + \bar{C}_A + \bar{C}_B + \bar{C}_R$$

Substituting for $\bar{C}_A$, $\bar{C}_B$ and $\bar{C}_R$ from Equations 3, 7 and 4,

respectively, in Equation 9 gives:

$$\bar{C}_M = \bar{C}_V + K_A C_A \bar{C}_V + \frac{K_B \bar{C}_V C_R}{K C_A} + K_R C_R \bar{C}_V$$

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Q. 3a

$$\bar{C}_m = \bar{C}_v \left(1 + K_A C_A + \frac{K_B C_R}{K C_A} + K_R C_R \right)$$

$$\therefore \bar{C}_v = \frac{\bar{C}_m}{1 + K_A C_A + \frac{K_B C_R}{K C_A} + K_R C_R} \quad (\text{Equation 10})$$

With this expression for $\bar{C}_v$ substituted in Equation 8, the final rate equation for adsorption of B as the rate limiting step is :

$$r_b = r = \frac{k_b \bar{C}_m \left[C_B - (1/K) (C_R/C_A) \right]}{1 + K_A C_A + (K_B/K) (C_R/C_A) + K_R C_R} \quad (\text{Equation 11})$$

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Q. 3 (b)

For pure A, 1 volume of feed on complete conversion yields 4 volumes of product mixture. Therefore, the fractional change in volume of the reaction system is

$$\epsilon_A = \frac{4 - 1}{1} = 3$$

For a plug flow behaviour, the performance equation is

$$\frac{W}{F_{A0}} = \int_0^{X_A} \frac{dX_A}{-r_A}$$

$$-r_A = 96.55 C_A = k' C_A, \quad k' = 96.55 \text{ l / (h. kg cat)}$$

For a variable density system, the concentration and conversion are related by

$$C_A = \left(\frac{1 - X_A}{1 + \epsilon_A X_A} \right) C_{A0}$$

For pure A at 3.2 atm and 117 °C,

$$C_{A0} = \frac{P_{A0}}{RT}$$

$$P_{A0} = \text{total pressure} = 3.2 \text{ atm} \dots\dots\dots \text{for pure A feed}$$

$$R = 0.08206 \text{ l.atm / (mol. K)}$$

$$T = 117^\circ\text{C} = 390 \text{ K}$$

$$C_{A0} = \frac{3.2}{0.08206 \times 390} = 0.1 \text{ mol/l}$$

$$\begin{aligned} \frac{W}{F_{A0}} &= \int_0^{X_A} \frac{dX_A}{-r_A} = \int_0^{X_A} \frac{dX_A}{k' C_A} \\ &= \frac{1}{k' C_{A0}} \int_0^{X_A} \left(\frac{1 + \epsilon_A X_A}{1 - X_A} \right) dX_A \end{aligned}$$

Integrating the above equation, we get

$$\begin{aligned} \frac{W}{F_{A0}} &= \frac{1}{k' C_{A0}} \left[(1 + \epsilon_A) \ln \left(\frac{1}{1 - X_A} \right) - \epsilon_A X_A \right] \\ W &= \frac{F_{A0}}{k' C_{A0}} \left[(1 + \epsilon_A) \ln \left(\frac{1}{1 - X_A} \right) - \epsilon_A X_A \right] \end{aligned}$$

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Page-9 Q.3 (b)

where : $k' = 96.55 \text{ l/(h. kg cat)}$

$$C_{A0} = 0.10 \text{ mol/l, } X_A = \frac{35}{100} = 0.35$$

$$\varepsilon_A = 3, F_{A0} = 2000 \text{ mol/h}$$

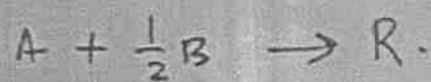
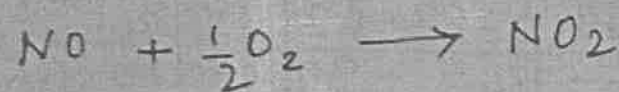
$$\begin{aligned} W &= \frac{2000}{96.55 \times 0.10} \left[(1 + 3) \ln \left(\frac{1}{1 - 0.35} \right) - 3 \times 0.35 \right] \\ &= 207.146 [1.723 - 1.05] \\ &= 139.41 \text{ kg} \end{aligned}$$

Amount of catalyst needed in the packed bed reactor = 139.41 kg

Example 6.15 . . .

(10)

Page-10 Q. 4 (a)



$$P = \text{total pr} = 3 \text{ atm.}$$

$$\text{sp. gr. of catalyst} = 0.48.$$

$$\therefore \text{Bulk density of cat.} = 0.48 \times 1000 \\ = 480 \text{ kg/m}^3.$$

$$\text{Flow rate of NO} = 50 \text{ metric tonnes per day.}$$

$$= 50 \times 10^3 \text{ kg/day}$$

$$= \frac{50 \times 10^3}{24} \text{ kg/hr}$$

$$= 2083.3 \text{ kg/hr.}$$

$$\text{Molar flow rate of NO to the reactor}$$

$$= \frac{2083.3}{30} = 69.44 \frac{\text{kmol}}{\text{hr.}}$$

(Mol. wt. of NO)

$$= 14 + 16$$

$$= 30$$

(Atomic weights)

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Q. 4 (a)

K.K.

Ans. No. mixture to the reactor contain 15 moles of NO.

Molar flow rate of NO to the reactor = 69.44 kmol/hr

(15% NO)

$$\frac{\text{Molar flow rate of } ^{85}\text{Ar}}{85\%} = \frac{\text{Molar flow rate of NO}}{15\%}$$

$$\therefore \text{Molar flow rate of air} = \frac{69.44 \times 85}{15}$$

$$(N_2 + O_2) = 393.49 \text{ kmol/hr}$$

$$O_2 \text{ in air} = 0.21 \times 393.49 = 82.63 \text{ kmol/hr}$$

$$\therefore \text{Total molar flow rate} = 69.44 + 393.49$$

$$= 462.93 \text{ kmol/hr}$$

Moles at time t, at conv. 90%.

$$\text{Moles of NO} = \cancel{69.44} - \frac{F_{NO}}{F_{NO}} \times 69.44$$

$$\text{Moles of NO} = 69.44 \text{ kmol/hr}$$

$$\text{Moles of } O_2 = 393.49 - \frac{1}{2} \times 69.44$$

$$= \text{Initial moles of } O_2 - \text{Reacted moles}$$

$$= 393.49 - \frac{1}{2} (0.9 \times 69.44)$$

$$= 371.38 \text{ kmol/hr}$$

Marks Awarded

$$F_{O_2} = \frac{1}{2} (0.9 \times 69.44)$$

$$\text{Moles of } NO_2 = \frac{1}{2} (0.9 \times 69.44) = \frac{1}{2} \times 62.496$$

$$= 31.248 \text{ kmol/hr}$$

$$\therefore \text{Total moles} = 31.248 + 31.248 + 62.496$$

=

$$N_2 \text{ in air} = 0.79 \times 393.49$$

$$= 310.86 \text{ kmol/hr}$$

$$\text{Total moles} = (\text{moles of } N_2) + (\text{moles of } O_2)$$

$$+ (\text{moles of } NO_2) + (\text{moles of } N_2)$$

$$= 69.44 + 31.248 + 310.86 + 62.496$$

$$\text{Total moles} = 432.13 \text{ kmol/hr}$$

$$\text{P.P. of } NO, P_{NO} = \left(\frac{69.44}{432.13} \right) \times 3$$

$$P_{NO} = 0.048 \text{ atm}$$

$$\therefore \text{P.P. of } O_2, P_{O_2} = \left(\frac{371.38}{432.13} \right) \times 3, P_{O_2} = 0.357 \text{ atm}$$

$$\text{P.P. of } NO_2, P_{NO_2} = \frac{62.496}{432.13} \times 3 = 0.437 \text{ atm}$$

$$P_{NO_2} = 0.437 \text{ atm}$$

$$69.44 + 31.248 = 100.688$$

$$100.688 = (35.32 + 69.44)$$

Marks

KK

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Q. 4 (a)

$$(-r') = \frac{100 - 0.2}{a + b P_{NO}^2 + c P_{NO_2}}$$

$$(-r') = 0.06947 \frac{\text{mol}}{\text{g. cat.} \cdot \text{hr}} = 0.06947 \frac{\text{kmol NO converted}}{\text{kg. cat.} \cdot \text{hr.}}$$

$$\text{wt. of catalyst} = \frac{\text{molar feed rate of NO}}{\text{Reaction rate}}$$

$$= \frac{69.44}{0.06947} \frac{\text{kg of cat.}}{\text{hr}} \left(\frac{\text{kmol NO converted} / \text{kg cat.} \cdot \text{hr}}{\text{kmol NO converted} / \text{kg cat.} \cdot \text{hr}} \right)$$

$$\text{wt. of cat.} = 999.6 \text{ kg}$$

$$\text{Volume of reactor} = \frac{\text{wt. of cat.}}{\text{Bulk den of cat.}}$$

$$= \frac{999.6}{480}$$

$$\text{Vol. of Reactor} = 2.08 \text{ m}^3$$

$$\text{Vol. of reactor} = \text{Vol. of cat.} = 2.08 \text{ m}^3$$

$$\frac{W}{F_{A0}} = \frac{\int_0^{x_A} \frac{r_A dx_A}{(-r_A)}$$

$$\frac{W}{F_{A0}} = \int_0^{0.40} \frac{dx_A}{(-r_A)}$$

$$\frac{W}{F_{A0}} = \frac{x_A}{(-r_A)}$$

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Q.5 (a)

Solution : Time required for complete conversion = $\tau = 20$ min

Mean residence time of solids in the bed = $\bar{t} = 48$ min

(i) **Chemical reaction step is rate controlling.**

For particles of single unchanging size in a fluidised bed with chemical controlling, we have :

$$1 - \bar{X}_B = \frac{1}{4} \left(\frac{\bar{t}}{\tau} \right) - \frac{1}{20} \left(\frac{\bar{t}}{\tau} \right)^2 + \frac{1}{120} \left(\frac{\bar{t}}{\tau} \right)^3 - \dots$$

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Q. 5 (a)

$$\tau = 20 \text{ min}, \bar{t} = 48 \text{ min}, \therefore \frac{\tau}{\bar{t}} = \frac{20}{48} = 0.4167$$

$$\begin{aligned} 1 - \bar{X}_B &= \frac{1}{4} (0.4167) - \frac{1}{20} (0.4167)^2 + \frac{1}{120} (0.4167)^3 \\ &= 0.096 \end{aligned}$$

The fraction of the original ore remaining unconverted ($1 - \bar{X}_B$) is 0.096 or 9.6%

(ii) Ash diffusion step is rate controlling :

For this mechanism the mean value for the fraction of solids unconverted is given

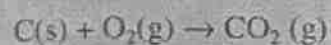
$$1 - \bar{X}_B = \frac{1}{5} \left(\frac{\tau}{\bar{t}} \right) - \frac{19}{420} \left(\frac{\tau}{\bar{t}} \right)^2 + \frac{41}{4620} \left(\frac{\tau}{\bar{t}} \right)^3 - \dots$$

$$\text{where } \frac{\tau}{\bar{t}} = 0.4167$$

$$\begin{aligned} 1 - \bar{X}_B &= \frac{1}{5} (0.4167) - \frac{19}{420} (0.4167)^2 + \frac{41}{4620} (0.4167)^3 \\ &= 0.076 \end{aligned}$$

The fraction of the original ore remaining unconverted ($1 - \bar{X}_B$) is 0.076 or 7.6%

Solution : Here the reacting particle shrinks during reaction and finally disappears.



From the reaction, $b = 1$

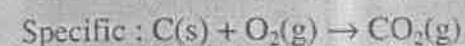
Given : $R = 12 \text{ mm} = 1.2 \text{ cm}$

$\rho_B = 2.4 \text{ g/cm}^3$

Molar density of graphite (C) = $\rho_B = \frac{2.4}{12} = 0.2 \text{ mol/cm}^3$

Given : $T = 900^\circ\text{C} = 1173 \text{ K}$, $P = 1 \text{ atm}$.

O_2 in the gas stream = 12% by volume



General : $b \text{ B(s)} + \text{A(g)} \rightarrow \text{fluid product}$

Comparing the above two equations, we get $b = 1$ and $\text{A} = \text{O}_2$

C_{Ag} - concentration of O_2 in the bulk gas phase

For an ideal gas : mole % = volume %

$\therefore$ Mole % O_2 in the gas stream = 12

We know :

$$P_{Ag} = x_A \cdot P = \frac{12}{100} \times 1 = 0.12 \text{ atm.}$$

The concentration of O_2 is calculated using the relation :

$$\begin{aligned} C_{Ag} &= \frac{P_{Ag}}{RT}, \quad R = 82.06 \text{ (cm}^3 \cdot \text{atm)/mol.K} \\ &= \frac{0.12}{82.06 \times 1173} \\ &= 1.25 \times 10^{-6} \text{ mol/cm}^3 \end{aligned}$$

Given : $k'' = 25 \text{ cm/s}$

Given : Negligible gas film resistance.

Therefore, for the shrinking spherical particle, in our case, chemical reaction controls the rate.

For the situation where chemical reaction controls, we have for shrinking sphere :

$$\begin{aligned} \tau &= \frac{\rho_B R}{b k'' C_{Ag}} = \frac{0.2 \times 12}{1 \times 25 \times 1.25 \times 10^{-6}} \\ &= 7680 \text{ s} \end{aligned}$$

Time required for the complete conversion of graphite particles of size $R = 12 \text{ mm}$ = 7680 s

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$$F_g = 90000 \text{ mol/h}, \quad F_l = 900000 \text{ mol/h.}$$

$$b = 1, p_{A1} = 100 \text{ Pa}, \quad C_{B1} = 55.56 \text{ mol/m}^3$$

$$C_T \approx C_U = 55556 \text{ mol/m}^3, \quad \pi = 10^5 \text{ Pa}$$

$$p_A - 100 = \frac{900000 \times 10^5}{90000 \times 1 \times 55556} (55.56 - C_B)$$

$$p_A = 1100 - 18 C_B$$

$$\text{or} \quad C_B = 61.11 - 0.0555 p_A$$

Now we will find C_{B2} in the exit stream.

$$p_A = p_{A2} = 1000 \text{ Pa}$$

$$\text{and} \quad C_{B2} = 61.11 - 0.0555 p_{A2}$$

$$\therefore C_{B2} = 61.11 - 0.0555 (1000) = 5.61 \text{ mol/m}^3$$

Let us now find the form of rate equation to be used :

$$k_{Ag} a = 0.36 \text{ mol/(h.m}^3.\text{Pa)}$$

$$k_{Al} a = 72 \text{ h}^{-1}, \quad a = 100 \text{ m}^2/\text{m}^3$$

$$\therefore k_{Al} = \frac{k_{Al} a}{a} = \frac{72}{100} = 0.72 \text{ m/h}$$

$$\mathcal{Q} = \mathcal{Q}_{B1} = \mathcal{Q}_{A1} = 3.6 \times 10^{-6} \text{ m}^3/\text{h}$$

$$k = 2.6 \times 10^7 \text{ m}^3/(\text{mol.h})$$

$$H_A = 10^5 (\text{Pa.m}^3)/\text{mol}$$

At the top of the tower :

$$p_A = p_{A1} = 100 \text{ Pa and } C_B = C_{B1} = 55.56 \text{ mol/m}^3$$

$$M_H = \frac{(\mathcal{Q}_{A1} C_B k)^{1/2}}{k_{Al}}$$

$$= \frac{(3.6 \times 10^{-6} \times 55.56 \times 2.6 \times 10^7)^{1/2}}{0.72} = 100$$

$$E_i = 1 + \frac{\mathcal{Q}_{B1} C_B H_A}{\mathcal{Q}_{A1} p_{A1}} = 1 + \frac{C_B H_A}{p_{A1}}$$

For $p_{A1} = 100 \text{ Pa}$ - liquid-film controls

For no gas-phase resistance : $p_{A1} = p_A = 100 \text{ Pa}$ and in this case

$$E_i = 1 + \frac{55.56 \times 10^5}{100} = 55560$$

Here $E_i \gg 5$ for any other small value of p_{A1} : $E_i > 5 M_H$

At the bottom of the tower :

$$p_A = p_{A2} = 1000 \text{ Pa}, C_B = C_{B2} = 5.61 \text{ mol/m}^3$$

$$M_H = \frac{(3.6 \times 10^{-6} \times 5.61 \times 2.6 \times 10^7)^{1/2}}{0.72} = 31.83$$

Assume $p_{Ai} = p_A = 1000 \text{ Pa}$

$$E_i = 1 + \frac{C_B H_A}{p_{Ai}} = 1 + \frac{5.61 \times 10^5}{1000} = 561$$

Here also $E_i > 5 M_H$ and for any other small value of p_{Ai} : $E_i > 5 M_H$.

$\therefore$ At both ends of the tower, we have : $E_i > 5 M_H$.

As we have $E_i > 5 M_H$ at both ends of the tower, we have a pseudo first-order reaction by gas-liquid interface and for this $E = M_H$.

It is a case of fast reaction with high C_B , the reaction zone is (near) by the interface in the liquid film.

For this case, the form of rate equation to be used is

$$(-r_A) a = -r_A''' = \frac{1}{\frac{1}{k_{Ag} a} + \frac{H_A}{a \sqrt{D_{Al} k C_B}}} p_A$$

or

$$-r_A''' = \frac{1}{\frac{1}{k_{Ag} a} + \frac{H_A}{k_{Al} a E}} \text{ with } E = M_H = \frac{\sqrt{D_{Al} k C_B}}{k_{Al}}$$

As M_H is different at the top and the bottom, the rate also varies and so we have to adopt a graphical procedure determine the tower height.

For graphical procedure, in addition to p_{A1} and p_{A2} take two additional p_A values and evaluate C_B at these values and then the rate and tabulate.

We have

$$C_B = 61.11 - 0.0555 p_A$$

Use the above equation to evaluate C_B

$$\text{For } p_A = 300 \text{ Pa}, C_B = 44.46 \text{ mol/m}^3$$

$$\text{For } p_A = 500 \text{ Pa}, C_B = 33.61 \text{ mol/m}^3$$

$$\text{For } p_A = 750 \text{ Pa}, C_B = 19.48 \text{ mol/m}^3$$

Now we will estimate the rate :

$$\text{For } p_A = 100 \text{ Pa},$$

$$D_{Al} = 3.6 \times 10^{-6} \text{ m}^2/\text{h},$$

$$H_A = 10^5 (\text{Pa} \cdot \text{m}^3)/\text{mol},$$

$$k_{Ag} = 0.36 \text{ mol}/(\text{h} \cdot \text{m}^2 \cdot \text{Pa})$$

$$C_B = 55.56 \text{ mol/m}^3$$

$$k = 2.6 \times 10^7 \text{ m}^3/(\text{mol} \cdot \text{h})$$

$$a = 100 \text{ m}^2/\text{m}^3$$

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$$-r_A'' = (-r_A') a = \frac{100}{\frac{1}{0.36} + \frac{10^5}{100 \sqrt{3.6 \times 10^{-6} \times 2.6 \times 10^7 \times 55.56}}}$$

$$= 6 \text{ mol/(h.m}^3\text{)}$$

Calculate the rate for other p_A values and tabulate :

p_A	C_B	$1/k_{Ag} a$	$H_A/a (\mathcal{Q}_{AI} k C_B)^{1/2}$	$-r_A''$	$\frac{1}{(-r_A'')}$
100	55.56	2.78	13.87	6	0.167
300	44.46	2.78	15.50	16.41	0.061
500	33.61	2.78	17.83	24.26	0.041
750	19.48	2.78	23.41	28.64	0.035
1000	5.61	2.78	43.64	21.54	0.046
200	50.61	2.78	14.62	11.5	0.087

The volume of tower (for dilute systems) is given by

$$V_r = \frac{F_g}{\pi} \int_{p_{A1}}^{p_{A2}} \frac{dp_A}{(-r_A'') a} = \frac{F_g}{\pi} \int_{p_{A1}}^{p_{A2}} \frac{dp_A}{-r_A''}$$

$$V_r = \frac{F_g}{\pi} \int_{100}^{1000} \frac{dp_A}{-r_A''}$$

To evaluate the integral on the RHS of the above equation, plot $\frac{1}{(-r_A'') a}$ i.e., $\frac{1}{(-r_A'') a}$ v/s p_A and measure the area under the curve between $p_A = p_{A1} = 100$ Pa and $p_A = p_{A2} = 1000$ Pa.

From the plot [Fig. Ex 3.8 (b)] :

Area under the curve = $1880 \text{ mm}^2 = 18.80 \text{ cm}^2$.

$$\therefore V_r = \frac{F_g}{\pi} \times \text{Area under the curve} \times \text{scale of x-axis} \times \text{scale of y-axis}$$

$$= \frac{90000}{10^5} \times 18.80 \times \frac{100}{1} \times \frac{0.05}{2}$$

$$= 42.3 \text{ m}^3$$

Volume of the tower required for the countercurrent operation = 42.3 m^3

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