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S.Y.B.Sc. (SEM-III) Paper I - USST401 SET-3

All questions are compulsory.

Figures to the right indicate full marks.

Use of calculator is allowed.

Q.1		Attempt all sub-questions: 2M each	(20)
	a.	State TRUE or FALSE and correct if necessary.	(10)
	i.	True	
	ii.	True	
	iii.	False.	
		For Normal distribution with parameters $(\mu=5, \sigma^2=100)$, μ_5 is 0.	
	iv.	False. X ~ Normal $(\mu = 18, \sigma^2 = 25)$, then the height ^{peak} of the Normal probability curve is highest at 18.	
	v.	False. The mode of F distribution is always less than 1	
	b.	Answer the following : 2M each	(10)
	i.	$f(x) = 1/10 \quad -5 < x < 5$ $= 0 \quad \text{Otherwise}$	
	ii.	X ~ Normal $(\mu = 32, \sigma^2 = 4)$, $Q_3 = \mu + 0.6745 \sigma = 33.349$	
	iii.	X has MGF $\exp\{4t + 18t^2\}$ X ~ Normal $(\mu = 4, \sigma^2 = 36)$	
	iv.	Mean = 9 variance = 18	
	v.	Variance = 5/3	
Q.2		Attempt any TWO sub-questions:	(20)
	a.	M.G.F. = $[e^{bt} - e^{at}] / t (b-a)$ 3M $\mu_r^1 = [b^{r+1} - a^{r+1}] / ((b-a)(r+1))$ 3M Mean = $(b+a) / 2$ 2M Variance = $(b-a)^2 / 12$ 2M	(10)
	b.	If X ~ Gamma (a) M.G.F. = $(1-t)^{-a}$ 5M Mean = a 2M Variance = a 3M	(10)
	c.	M.G.F. = $2/t^2 \{ [e^{at} / (a-b)(a-c)] + [e^{ct} / (c-a)(c-b)] + [e^{bt} / (b-a)(b-c)] \}$ 10M	(10)
Q.3		Attempt any TWO sub-questions:	(20)
	a.	X ~ Normal (μ, σ^2) Mean = $E(X) = \mu$ 5M Variance = $E(X - \mu)^2 = \sigma^2$ 5M	(10)

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	b.	<p>$X \sim \text{Normal}(\mu, \sigma^2)$</p> <p>M.G.F. = $M_X(t) = e^{\mu t + \frac{1}{2}\sigma^2 t^2}$4M</p> <p>C.G.F. = $\log_e M_X(t) = \mu t + \frac{1}{2}\sigma^2 t^2$1M</p> <p>$\mu_1 = \mu, \mu_2 = \sigma^2, \mu_3 = 0, \mu_4 = 3\sigma^4$2M</p> <p>Measures of skewness $\beta_1 = 0, \gamma_1 = 0$ symmetric</p> <p>Measures of kurtosis $\beta_2 = 3, \gamma_2 = 0$ mesokurtic</p> <p>.....3M</p>	(10)
	c.	<p>i.</p> <p>$X \sim \text{Normal}(\mu_1, \sigma_1^2)$</p> <p>$Y \sim \text{Normal}(\mu_2, \sigma_2^2)$</p> <p>M.G.F. = $e^{\mu t + \frac{1}{2}\sigma^2 t^2}$1M</p> <p>Distribution of X+Y</p> <p>$M_{X+Y}(t) = M_X(t) \times M_Y(t) = e^{\mu_1 t + \frac{1}{2}\sigma_1^2 t^2} \times e^{\mu_2 t + \frac{1}{2}\sigma_2^2 t^2}$</p> <p>$= e^{(\mu_1 + \mu_2)t + \frac{1}{2}(\sigma_1^2 + \sigma_2^2)t^2}$</p> <p>$X+Y \sim \text{Normal}(\mu_1 + \mu_2, \sigma_1^2 + \sigma_2^2)$2M</p> <p>Distribution of X-Y</p> <p>$M_{X-Y}(t) = M_X(t) \times M_Y(-t) = e^{\mu_1 t + \frac{1}{2}\sigma_1^2 t^2} \times e^{\mu_2(-t) + \frac{1}{2}\sigma_2^2 t^2}$</p> <p>$= e^{(\mu_1 - \mu_2)t + \frac{1}{2}(\sigma_1^2 + \sigma_2^2)t^2}$</p> <p>$X-Y \sim \text{Normal}(\mu_1 - \mu_2, \sigma_1^2 + \sigma_2^2)$2M</p>	(05)
		<p>ii.</p> <p>$X \sim \text{Normal}(\mu, \sigma^2)$</p> <p>Median = μ1M</p> <p>Mean deviation about median = $\sqrt{\frac{2}{\pi}} \sigma$4M</p>	(05)
Q.4		Attempt any TWO sub-questions:	(20)
	a.	<p>Pdf 1M</p> <p>M.G.F. = $(1 - 2t)^{-n/2}$ 4M</p> <p>C.G.F.1M</p> <p>Mean = n 2M</p> <p>Variance = $2n$ 2M</p> <p>Where n is degrees of freedom</p>	(10)
	b.	Derivation 10M	(10)
	c.	<p>$\mu_r = (f_2/f_1)^r \Gamma(f_1/2 + r) \Gamma(f_2/2 - r) / \Gamma(f_1/2) \Gamma(f_2/2)$7 M</p> <p>Mean = $f_2 / f_2 - 2$ 3M</p> <p>Where r.v. follows F distribution with (f_1, f_2) degrees of</p>	(10)

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		freedom.	
Q.5		Attempt any TWO sub-questions:	(20)
a.		M.G.F. = $(\theta / \theta - t)$ C.G.F. = $\log_e (\theta / \theta - t)$ Mean = $1/\theta$ Variance = $1/\theta^2$	(10)
b.	i.	$X \sim \text{Normal} (\mu, \sigma^2)$ Mode of Normal distribution = μ5M	(05)
	ii.	Any five properties of Normal distribution with parameters of (μ, σ^2)5M	(05)
c.		Mean deviation = $f^{1/2} \Gamma (f/2 - 1/2) / \Gamma(1/2) \Gamma(f/2)$, 10M	(10)
