

① sem III - Stats II

Q1. (a)

- (i) Prob. of an event always lies between 0 and 1.
- (ii) $P(\text{exactly 2 heads}) = 3/8$
- (iii) $P(A \cup B) = 2/3$
- (iv) $\sum P(x) = 1$
- (v) $V(c) = 0$
- (vi) $p = 3/5$
- (vii) Poisson distribution

(b)

- (i) Sample space - defⁿ ①
example ①
- (ii) Exhaustive events - defⁿ - ②
- (iii) $P(A^c) = \frac{b}{a+b}$
- (iv) $E(3X-4) = 41$
- (v) measure of skewness $B_1 = \frac{\mu_3^2}{\mu_2^3}$
- (vi) prob. of success p is small, $p \rightarrow 0$, number of trials is large $n \rightarrow \infty$, but mean np is finite, binomial distⁿ \rightarrow Poisson distⁿ.
- (vii) Mean of Hypergeometric distⁿ $= \frac{Mn}{N}$

② marks each.

Q.2 (a) Defⁿ - ② marks each

(b)

$$(i) S = \{1, 2, 3, \dots, 20\} \quad - ①$$

$$A = \{3, 6, 9, 12, 15, 18, 5, 10, 20\} \quad - ①$$

$$P(A) = \frac{n}{N} = \frac{9}{20} \quad - ②$$

$$(ii) P(A) = \frac{1}{n} \quad P(\bar{A}) = \frac{2}{n}$$

1. P(target remains unhit)

$$= P(\bar{A} \cap \bar{B}) = \frac{2}{3} \cdot \frac{3}{4} = \frac{1}{2} \quad - (1)$$

2. P(target is hit)

$$= P(A \cup B)$$

$$= \frac{1}{3} + \frac{1}{4} - \frac{1}{3} \cdot \frac{1}{4} = \frac{1}{2} \quad - (2)$$

3. P(only one of them hits the target)

$$= P(A \cap \bar{B}) + P(\bar{A} \cap B)$$

$$= \frac{5}{12} \quad - (2)$$

(c)

(i) Prob. of an event - explanation (1)

- definition (2)

- assumptions (2)

(ii) A card is drawn from a pack of 52 cards

(i) $P(\text{queen} / \text{face card}) = 4/12 = 1/3 \quad - (2)$

(ii) $P(\text{queen} / \text{heart card}) = 1/13 \quad - (1)$

(iii) $P(\text{queen} / \text{not a jack}) = 4/48 = 1/12 \quad - (2)$

Q.3. (a)

(i) Defⁿ cumulative distrⁿ fun. (2)

important properties any three (3)

(ii) mean of $X = E(X) = \sum x \cdot p(x)$

$$= 0.7 \quad - (2)$$

$$E(X^2) = \sum x^2 \cdot p(x) = 1.3 \quad - (1)$$

$$V(X) = E(X^2) - [E(X)]^2$$

$$= 0.81 \quad - (2)$$

(b) (i) Raw moment (1)

central moment (1)

Relationship μ_1, μ_2, \dots (1 mark each)

μ_3

(2)

3

3

Q. 3. (b)

(i)

$$1. E(4X + 2Y + 5) = 4(10) + 2(20) + 5 = 85 \quad - (2)$$

$$2. V(3X + 2Y) = 9 \cdot V(X) + 4 \cdot V(Y) + 2 \cdot 3 \cdot 2 \cdot 2$$

$$= 9(4) + 4(16) + 24$$

$$= 124 \quad - (2)$$

(c)

Definitions - (2) marks each

When do we say X and Y are indep. - (2)

effect of indep. on ~~conditional~~ conditional distn - (2)

Q. 4 (a)

Defn - $X \sim$ Uniform - (2)

prob. distn of X denoting number on the uppermost face of a die - (3)

$E(X)$ - (2)

$V(X)$ - (3)

(b)(i) Bernoulli trials - (2)

Binomial prob. law - (2)

properties - (2)

(ii) mean = $np = 3$

$$15. P(X=0) = 2 \cdot P(X=1)$$

$$q = 2/5 \quad p = 3/5 \quad n = 5 \quad - (2)$$

$$P(X=5) = {}^5C_5 \left(\frac{3}{5}\right)^5 \left(\frac{2}{5}\right)^0 = 0.07776 \quad - (2)$$

(c)

(i) Hypergeometric distn - defn - (3)

Conditions

(ii) X : no. of calls received during an interval of 10 minutes

$$X \sim P(m=1) \quad - (1)$$

$$1. P(X=0) = 0.36788 \quad - (2)$$

$$2. P(X=2) = 0.18394 \quad - (2)$$

Q.5. (a)

(i) Multiplication thmⁿ - statement $- (2)$

- Proof $- (3)$

$$\left. \begin{array}{l} (ii) A: \text{fiction} \quad P(A) = 0.40 \\ B: \text{Biography} \quad P(B) = 0.30 \end{array} \right\} \quad - (1)$$

$$P(A \cap B) = 0.20 \quad - (1)$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B) \quad - (1)$$

$$= 0.40 + 0.30 - 0.20$$

$$= 0.5 \quad - (2)$$

(b)

$$(i) E(ax+b) = aE(x) + b \quad - (2)$$

$$V(ax+b) = a^2 V(x) \quad - (3)$$

$$\begin{aligned} (ii) F(x) &= 0 & x < -3 \\ &= 0.1 & -3 \leq x < -1 \\ &= 0.3 & -1 \leq x < 0 \\ &= 0.45 & 0 \leq x < 1 \\ &= 0.65 & 1 \leq x < 2 \\ &= 0.75 & 2 \leq x < 3 \\ &= 0.90 & 3 \leq x < 5 \\ &= 0.95 & 5 \leq x < 8 \\ &= 1 & x \geq 8 \end{aligned} \quad - (4)$$

$$P(-1 \leq X \leq 2) = 0.45 \quad - (1)$$

(c) (i) Statement - recurrence relation $- (1)$

Proof $- (4)$

$$(ii) n=100, \quad p=0.03$$

$$m=7, \quad p=3 \quad - (1)$$

$$X: \text{no. of defectives} \sim P(m=3) \quad - (2)$$

$$P(X > 4) = 1 - P(X \leq 4) = 0.1847 \quad - (2)$$

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