

FYBBI - Quantitative Methods - I

Q.P Code :- 57613 Date :- 30/3/2019
 (75 marks)

QIA] Multiple Choice Question (8)

01 → (b) ; 02 → (a) ; 03 → (a) ; 04 → (b)
 05 → (a) ; 06 → (b) ; 07 → (a) ; 08 → (a)
 09 → (b) ; 10 → (a)

QIB) Match the following (7)

01 → (i) ; 02 → (c) ; 03 → (a) ; 04 → (b)
 05 → (d) ; 06 → (e) ; 07 → (f) ; 08 → (g)
 09 → (j) ; 10 → (h)

(08)

Q2A) CI	freq	C.f	
10-20	9	9	
20-30	5	14	→ Q ₁
30-40	11	25	
40-50	12	37	→ Q ₃
50-60	<u>3</u>	<u>40</u>	
	40		

$$q_1 = \frac{N}{4} = \frac{40}{4} = 10$$

$$\begin{aligned} Q_1 &= l_1 + \frac{q_1 - C}{f} (l_2 - l_1) \\ &= 20 + \frac{10 - 9}{5} (30 - 20) \\ &= \underline{\underline{22}} \end{aligned}$$

(P.T.O)

$$q_3 = \frac{3N}{4} = \frac{3 \times 40}{4} = 30$$

$$\begin{aligned} Q_3 &= l_1 + \frac{q_3 - c}{f} (l_2 - l_1) \\ &= 40 + \frac{30 - 25}{12} (50 - 40) \\ &= \underline{\underline{44.17}} \end{aligned}$$

$$\begin{aligned} \text{Quartile Deviation} &= \frac{Q_3 - Q_1}{2} \\ &= \frac{44.17 - 22}{2} = \underline{\underline{11.09}} \end{aligned}$$

$$\begin{aligned} \text{Coeff. of QD} &= \frac{Q_3 - Q_1}{Q_3 + Q_1} = \frac{44.17 - 22}{44.17 + 22} \\ &= \underline{\underline{0.34}} \end{aligned}$$

(07)

Q2B] wt in kg.	No of men	fx	x - $\bar{x}$	f x - $\bar{x}$
50	20	1000	12	240
55	15	825	7	105
60	25	1500	2	50
65	10	650	3	30
70	30	2100	8	240
	<u>100</u>	<u>6175</u>		<u>665</u>

$$\bar{x} = \frac{\sum fx}{\sum f} = \frac{6175}{100} = 61.75 \text{ i.e. } 62$$

$$M.D = \frac{\sum f|x - \bar{x}|}{\sum f} = \frac{665}{100} = \underline{\underline{6.65}}$$

Q2C]

x Demand Index	y Price Index	$(x - \bar{x})$	$(y - \bar{y})$	$(x - \bar{x})^2$	$(y - \bar{y})^2$	$(x - \bar{x})(y - \bar{y})$
100	98	-3	-11	9	121	33
102	115	-1	6	1	36	-6
104	108	1	-1	1	1	-1
106	115	3	6	9	36	18
<u>412</u>	<u>436</u>			<u>20</u>	<u>194</u>	<u>44</u>

$$\bar{x} = \frac{\sum x}{n} = \frac{412}{4} = 103 ; \bar{y} = \frac{\sum y}{n} = \frac{436}{4} = 109$$

$$\sigma_x = \sqrt{\frac{\sum (x - \bar{x})^2}{n}} ; \sigma_y = \sqrt{\frac{\sum (y - \bar{y})^2}{n}}$$

$$= \sqrt{\frac{20}{4}}$$

$$= \underline{\underline{2.24}}$$

$$= \sqrt{\frac{194}{4}}$$

$$= \underline{\underline{6.96}}$$

$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{n \cdot \sigma_x \cdot \sigma_y} = \frac{44}{(4)(2.24)(6.96)}$$

$$= \frac{44}{62.36} = \underline{\underline{0.71}}$$

Q2D]

$$b_{xy} = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (y - \bar{y})^2}$$

$$= \frac{350}{240} = \underline{\underline{1.46}}$$

$$b_{yx} = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

$$= \frac{350}{280} = \underline{\underline{1.25}}$$

$$\bar{x} = \frac{\sum x}{n} = \frac{200}{5} = 40$$

$$\bar{y} = \frac{\sum y}{n} = \frac{110}{5} = 22$$

i) Regression equation X on Y

$$(x - \bar{x}) = b_{xy} (y - \bar{y})$$

$$(x - 40) = 1.46 (y - 22)$$

$$\therefore x = 1.46y + 7.88$$

ii) Regression equation Y on X

$$(y - \bar{y}) = b_{yx} (x - \bar{x})$$

$$(y - 22) = 1.25 (x - 40)$$

$$y = 1.25x - 28$$

Q3A)

(8)

$$E(x) = \sum x_i P_i$$

$$= 0 \times 0.20 + 1 \times 0.25 + 2 \times 0.30 + 3 \times 0.15 + 4 \times 0.10$$

$$= \underline{1.7}$$

$$V(x) = E(x^2) - [E(x)]^2$$

$$E(x^2) = \sum (x_i)^2 P_i$$

$$= (0)^2 \times 0.20 + (1)^2 \times 0.25 + (2)^2 \times 0.30 + (3)^2 \times 0.15 + (4)^2 \times 0.10$$

$$= \underline{4.4}$$

$$\begin{aligned} \therefore V(x) &= 4.4 - (1.7)^2 \\ &= 4.4 - 2.89 \\ &= \underline{1.51} \end{aligned}$$

Q3B]

(7)

$$n(S) = {}^{52}C_1 = 52.$$

(i) Let A be the event of getting a heart
 $n(A) = {}^{13}C_1 = 13 \therefore P(A) = \frac{n(A)}{n(S)} = \frac{13}{52}$

ii) Let B be the event of getting a Queen
 $n(B) = {}^4C_1 = 4 \therefore P(B) = \frac{n(B)}{n(S)} = \frac{4}{52}$

ii) ~~n(A ∩ B)~~ =

$n(A \cap B)$ = a event of getting a Queen of hearts.

$$n(A \cap B) = {}^1C_1 = 1$$

$$\therefore P(A \cap B) = \frac{n(A \cap B)}{n(S)} = \frac{1}{52}$$

$$\therefore P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$\Rightarrow$ Addition Theorem

$$\begin{aligned} \therefore P(A \cup B) &= \frac{13}{52} + \frac{4}{52} - \frac{1}{52} \\ &= \frac{16}{52} = \underline{\underline{0.31}} \end{aligned}$$

Q3c]

CI	F	CF	
100-150	4	4	
150-200	7	11	— D ₂
200-250	20	31	
250-300	9	40	— P ₈₀
300-350	6	46	
350-400	4	50	
	50		

$$d_2 = \frac{2N}{10} = \frac{2 \times 50}{10} = 10$$

$$D_2 = d_1 + \frac{d_2 - c}{f} (d_2 - d_1)$$

$$= 150 + \frac{10 - 4}{7} (200 - 150)$$

$$= \underline{\underline{192.86}}$$

$$P_{80} = \frac{80 \times 50}{100} = \underline{\underline{40}}$$

$$P_{80} = d_1 + \frac{P_{80} - c}{f} (d_2 - d_1)$$

$$= 250 + \frac{40 - 31}{9} (300 - 250)$$

$$= \underline{\underline{300}}$$

Q3D]

Commodity	P_0	P_1	Q_0	$I = \frac{P_1}{P_0} \times 100$	$W = P_0 Q_0$
A	2	4	2	200	4
B	3	5	5	167	15
C	10	15	10	150	100
					<u>119</u>

 $\sum iw$

800

2505

1500

4805

$$\therefore P_{01} = \frac{\sum iw}{\sum w}$$

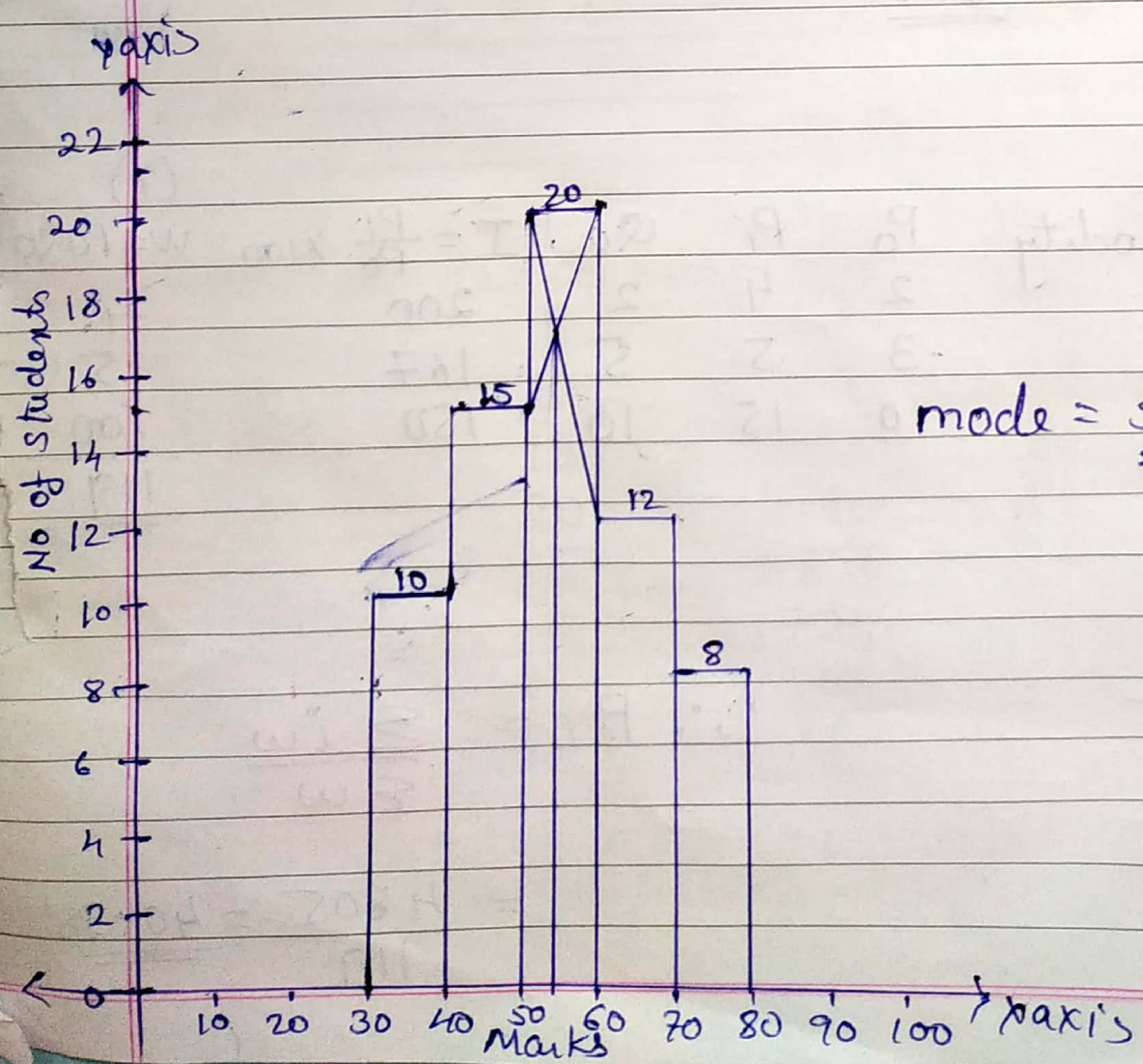
$$= \frac{4805}{119} = \underline{\underline{40.38}}$$

Q4A

CI	F	class width	class Mark	less than cf	more than cf	% frequency
100-105	15	5	102.5	15	40	37.5%
105-110	12	5	107.5	27	25	30%
110-115	7	5	112.5	34	13	17.5%
115-120	6	5	117.5	40	6	15%
	40					<u>100%</u>

Q4B

Scale :-
 x-axis = 1cm = 10 mark
 y-axis = 1cm = 2 student



Q4C)

Tabulated rate per ₹1000	55.30
(-) 4% Reduction	<u>(2.212)</u>
(-) ₹2 reduction per ₹1000	(2)

Annual premium per ₹1000 51.09

Annual premium for ₹3,00,000

$$= \frac{51.09}{1000} \times 3,00,000$$
$$= \underline{\underline{₹15,327}}$$

$$\text{Monthly premium} = \frac{15,327}{12} = \underline{\underline{₹1,277.25}}$$

Q4D]

Ht.in.cm	No of children	fx	cf	
110	8	880	8	
111	10	1110	18	
112	13	1456	31	
113	20	2260	51	- M
114	25	2850	76	
115	15	1725	91	
116	<u>9</u>	<u>1044</u>	100	
	100	<u><u>11325</u></u>		

$$(A.M) \bar{X} = \frac{\sum fx}{\sum f} = \frac{11325}{100} = \underline{\underline{113.25}}$$

$$\text{Median :- } \frac{N}{2} = \frac{100}{2} = 50$$

∴ cumulative frequency greater than $\frac{N}{2}$ is 50 is 51 and

the value of x corresponding to 51 is 113

∴ Median is 113