

Q.P. 52446.

①

Q.	ATTEMPT ANY FOUR FROM THE FOLLOWING	MARKS
I	A)	05
	i) $(5/x) + 6x$	
	ii) $[(\log x - 5)8x - (4x^2 + 3)/x]/(\log x - 5)^2$	
	B) $R = pD$, where $D = 300p - p^2$ $R = p(300p - p^2)$ $R = 300p^2 - p^3$ when $p = 5$ $T.R. = 300(5^2) - 5^3$ $T.R. = 300(25) - 125$ $T.R. = \text{Rs. } 7375$	05
	C) $C = 9 + 20x + x^2$ $AC = C/x = 9/x + 20 + x$ When $x = 3$ then $AC = 26$ $MC = dc/dx = 20 + 2x$ When $x = 3$ then $MC = 26$	05
	D) Since $D = 12 + 4p - p^2$ $dD/dp = 4 - 2p$ $\eta = (-p/D)(dD/dp)$ $= [-p/(12 + 4p - p^2)](4 - 2p)$ $= p(2p - 4)/(12 + 4p - p^2)$ η at $p = 3$ is given by $\eta = 3(6 - 4)/(12 + 12 - 9)$ $= 6/15 = 2/5$	05
	E) Given $R = 30x - x^2$ and $C = 20 + 4x$ Profit is given by $p = R - C$ $P = (30x - x^2) - (20 + 4x)$ $P = -20 + 26x - x^2$ $dp/dx = 26 - 2x$ & $d^2p/dx^2 = -2$ Now $dp/dx = 0$, if $26 - 2x = 0$ i.e. if $x = 13$ When $x = 13$, $d^2p/dx^2 = -2 < 0$ Thus for $x = 13$, $dp/dx = 0$ and $(d^2p/dx^2) < 0$ P is maximum when $x = 13$ Maximum profit when $x = 13$ $\text{Max } p = -20 + 26 \cdot 13 - 13^2$ $= -20 + 13(26 - 13)$ $= 13 \cdot 13 - 20 = 169 - 20 = 149$	05
Q2	A) Let rate will be x In first case, $p = 15000$ and $n = 4$ years $SI = Pni = 15000 \cdot 4 \cdot x = 60000x$ In case second, $p = 16000$, $n = 3$ years, $i = 0.1$ $SI = Pni = 16000 \cdot 3 \cdot 0.1 = 4800$ Therefor $60000x = 4800$ $X = 0.08$ Therefor Rate of interest is 8%	05

	B)	Given $p = \text{Rs } 30000$, $i = 0.1$, $n = 2$ years, $m = 2$ $A = P(1+i/m)^{mn}$ $A = (30000)(1.05)^4$ $A = (30000)(1.276)$ $A = \text{Rs } 38280$	05																																
	C)	Given $A = 50000$, $n = 3$ years, $r = 6\%$, $i = 0.06$ $A = P(1+i)^n$ $50000 = P(1.06)^3$ $P = \text{Rs } 41980.9642$	05																																
	D)	Given $C = \text{Rs } 20000$, $i = 0.1$, $n = 4$ years $A = C[(1+i)^n - 1]/i$ $= 20000[(1.1)^4 - 1]/0.1$ $= 20000(1.4641 - 1)$ $A = \text{Rs } 92820$	05																																
	E)	Given $P = \text{Rs } 80000$, $n = 4$ months $r = 12/12 = 1\% \text{ p.m.}$, hence $i = 0.01$ Let the EMI be C Rs $P = C[1 - (1+i)^{-n}]/i$ $80000 = C[1 - (1.01)^{-4}]/0.01$ $800 = C[1 - 0.96098]$ $= C[0.03902]$ $C = \text{Rs } 20502.3065$	05																																
Q3																																			
	A)	Given, $\bar{x} = \Sigma x/n = 3$ $\bar{y} = \Sigma y/n = 4$ $r = [(\Sigma xy/n) - \bar{x}\bar{y}] / [\sqrt{(\Sigma x^2/n) - \bar{x}^2}] [\sqrt{(\Sigma y^2/n) - \bar{y}^2}]$ $r = [(325/25) - 12] / [\sqrt{(250/25) - 9}] [\sqrt{(500/25) - 16}]$ $r = 0.5$	05																																
	B)	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Rank (X)</th> <th>Rank (Y)</th> <th>d</th> <th>d²</th> </tr> </thead> <tbody> <tr><td>2</td><td>1</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>5</td><td>-4</td><td>16</td></tr> <tr><td>3</td><td>6</td><td>-3</td><td>9</td></tr> <tr><td>4</td><td>4</td><td>0</td><td>0</td></tr> <tr><td>5</td><td>3</td><td>2</td><td>4</td></tr> <tr><td>6</td><td>2</td><td>4</td><td>16</td></tr> <tr> <td colspan="3"></td> <td style="text-align: center;">$\Sigma d^2 = 46$</td> </tr> </tbody> </table> <p style="margin-left: 20px;"> $R = \frac{1 - \frac{\Sigma d^2}{n^3 - n}}{1}$ $= \frac{1 - \frac{46}{6^3 - 6}}{1}$ $= 1 - 1.314285$ $R = -0.314285$ </p>	Rank (X)	Rank (Y)	d	d ²	2	1	1	1	1	5	-4	16	3	6	-3	9	4	4	0	0	5	3	2	4	6	2	4	16				$\Sigma d^2 = 46$	05
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(3)

	C)	<p>Let y=yield and x=Rainfall Given, $r=0.8$ $\bar{x}=27, \bar{y}=40$ $\sigma_x=3, \sigma_y=6$ $b_{yx}=r \sigma_y / \sigma_x$ $b_{yx}=1.6$ $y-\bar{y}=b_{yx}(x-\bar{x})$ $y-40=1.6(x-27)$ when $x=30$ then $y-40=1.6(30-27)$ $=4.8$ $Y=44.8$</p>	05																																																						
	D)	<p>Let regression line of y on x is $2x+3y-66=0$------(1) and regression line of x on y is $2x+y-38=0$------(2) we know that, $y-\bar{y}=b_{yx}(x-\bar{x})$------(3) and $3y=66-2x$ $y=22-(2/3)x$------(4) Comparing coefficients of x in equations 3 and 4 we get $b_{yx}=-2/3$ similarly, $2x=38-y$ $x=19-(1/2)y$------(5) and $x-\bar{x}=b_{xy}(y-\bar{y})$------(6) Comparing coefficients of x in equations 5 and 6 we get $b_{xy}=-1/2$ we know that, $r=\sqrt{(b_{yx} b_{xy})}$ $r=\sqrt{((-1/2)*(-2/3))}=\sqrt{0.333333}$ $r=0.5773$</p>	05																																																						
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	<p>B) $\lambda=2$ $P(x)=(e^{-\lambda}\lambda^x)/x!$ i) $P(x=0)=(e^{-2}\lambda^0)/0!=0.135$ ii) $P(\text{at most two successes})=P(0)+P(1)+P(2)$ $=0.135+(0.135*2)+(0.135*2)$ $=0.675$</p>	05
	<p>C) Given, $p=4/5, q=1/5, n=5$ $P(x)={}^nC_x p^x q^{n-x}$ i) $P(x=4)={}^5C_4(4/5)^4(1/5)^1$ $=5*0.4096*0.2$ $=0.4096$ ii) $P(1 \text{ or less})=P(0)+P(1)$ $={}^5C_0(4/5)^0(1/5)^5+{}^5C_1(4/5)^1(1/5)^4$ $=0.00672$</p>	05
	<p>D) Let X: weekly wages We know, standard normal variate Z $Z=(X-\mu)/\sigma$ Here, $\mu=770, \sigma=70$ $Z=(X-770)/70$ When $X=770, Z=0$ When $X=700, Z=(700-770)/70=-1$ Area to the left of $Z=-1$ $=(\text{Area to the left of } Z=0) - (\text{Area between } Z=0 \text{ \& } Z=-1)$ $=0.5-0.3413$ $=0.1587$ $P(X<700)=P(Z<-1)=0.1587$ The number of workers earning less than Rs 700=$N*P$ $=8000*0.1587$ $=1269.6$</p>	05