

Q.1a.

i) TRUE

ii) TRUE

iii) TRUE

iv) TRUE

v) False: Idle time is the time for which machine remains idle during total elapsed time.

Q.1B.

i) slack variable: If a constraint has \leq (less than or equal to sign) then in order to make equality. The non-negative quantity (variable) which is added to left hand side is called slack variable.

surplus variable: The non-negative quantity (variable) which is subtracted from the left hand side of the constraint to convert \geq greater than or equal to type constraint to equation.

ii)

$$\text{New element} = \text{old element} - \frac{\text{Key Row element} \times \text{Key Column element}}{\text{Key element}}$$

iii) Number of occupied cells = $m+n-1$

iv) Assigning n jobs to n persons with total cost for performing all jobs is minimum.

v) No passing rule means that passing is not allowed, i.e. the same order of jobs is maintained over each machine.

Q.2 a)

i) 05 marks

- standard form - (2 1/2 marks)

- canonical form - (2 1/2 marks)

ii) 05 marks.

x_1 : # of units of refrigerators

x_2 : # of units of ranges.

$$\max z = 60x_1 + 40x_2$$

$$s.t. \quad x_1 \leq 25$$

$$x_2 \leq 35$$

$$2x_1 + x_2 \leq 60$$

$$x_1, x_2 \geq 0$$

Q.2 b

i) - Dual procedure - 2 1/2 marks

ii) - Dual of Dual is primal - 2 1/2 marks

ii)

standard form

$$\max z = 3x_1 + 2x_2 + 0s_1 + 0s_2 - MA_1$$

s.t.

$$2x_1 + x_2 + s_1 = 12$$

$$3x_1 + 4x_2 - s_2 + A_2 = 12$$

Initial table.

CB	B	x_B	x_1	x_2	s_1	s_2	A_1	$\frac{x_B}{x_2}$
0	s_1	2	2	①	1	0	0	$2/4 = 2 \rightarrow$
-M	A_1	12	3	4	0	-1	1	$12/4 = 3$
	Z_j	-12M	-3M	4M	0	M	-M	
	$Z_j - C_j$	-	-3M-3	-4M-2	0	M	0	

since all $Z_j - C_j \leq 0$ current feasible solution is not optimum. the most negative $Z_j - C_j$ is $-4M-2$

$\therefore x_2$ variable enters in basis & s_1 leaves the basis.

x_1	x_2	x_3	x_4	s_1	s_2	A_1
2	2	2	1	1	0	0
$-m$	4	-5	0	-4	-1	1
Z_j	$4-4m$	$4+5m$	2	$2+4m$	m	$-m$
$Z_j - C_j$	$-5m$	0	$4m+2$	m	0	0

since all $Z_j - C_j > 0$ & artificial variable appears in the basis at positive level hence given LPP does not possess any feasible solⁿ.

Q.2 c. algorithm - 10 marks

Q.3 a) i) LPP in mathematical form - 04 marks

ii) Profit = return - transportation cost

Profit matrix

	D_1	D_2	D_3	D_4
A	6	6	6	4
B	4	2	4	5
C	5	6	7	8

cost matrix = max profit - profit

	D_1	D_2	D_3	D_4
A	2	2	2	4
B	4	6	4	3
C	3	2	1	0

	D_1	D_2	D_3	D_4	Capacity
A	200	800	12	14	1000
B	700	16	14	13	700
C	0	12	500	400	900
Demand	900	800	500	400	

(* solⁿ by using XAM method). If allocations = 5 < m+n-1 hence the solution is non-degenerate.

Q.3 b) i) Vogel's Approximation Method - 04 marks

ii)

	A	B	C	supply
1	5	7	4	5
2	3	6	1	8
3	5	4	7	7
4	1	6	2	14
Demand	7	9	18	34

NWC solution
 $x_{11}=5, x_{21}=2, x_{22}=6, x_{32}=3$
 $x_{33}=4, x_{43}=14$ Total cost = 102

1115 Least cost method.
 $x_{12}=2, x_{13}=3, x_{23}=8, x_{32}=7$
 $x_{41}=7, x_{43}=7$ Total cost = 83

Q.3 c) MODI method - 10 marks. (step by step procedure)

Q.4 a) i) Travelling Salesman problem ~~not~~ short note - 5 marks

ii)

converting maximization to minimization
(opportunity loss of maximum profit)

highest element is 14 subtracted from each element in 14.

		A	B	C	D	E
machine 1	5	11	10	12	4	
2	2	4	6	3	5	
3	3	12	5	14	6	
4	6	14	4	11	7	
5	7	3	8	12	5	

opportunity loss table

		A	B	C	D	E
Machine 1	9	3	4	2	10	
2	12	10	8	11	9	
3	11	2	9	0	8	
4	8	0	10	3	7	
5	7	5	6	2	2	

optimum assignment when applying assignment Hungarian method

machine 1 → C, machine 2 → E, machine 3 → D

machine 4 → B machine 5 → A.

Q.4 b

▷ ~~sort~~ sequencing Algorithm - 04 marks

ii)

optimal sequence :

A F D B C E

Job	machine A		machine B	
	In	out	In	out
A	0	1		
F	1	3	1	4
D	3	4	4	5
B	6	10	9	17
C	10	16	17	23
E	16	21	23	31
			31	32

Total elapsed time = 32 hours.

Q.4) step by step procedure of Hungarian method — 10 marks

Q.5a)

$$i) \min z = x_1 - x_2 + x_3$$

$$\text{s.t. } \begin{aligned} x_1 - x_2 &\geq 4 \\ x_1 - x_2 + 2x_3 &\geq 3 \\ x_1, x_2, x_3 &\geq 0 \end{aligned}$$

Dual
max

$$z' = 4w_1 + 3w_2$$

$$w_1 + w_2 \leq 1$$

$$0w_1 - w_2 \leq -1$$

$$-w_1 + 2w_2 \leq 1$$

$$w_1, w_2 \geq 0$$

Standard form

$$\max z' = 4w_1 + 3w_2 + 0s_1 - 0s_2 - M A_1$$

$$\text{s.t. } w_1 + w_2 + s_1 = 1$$

$$-w_2 - s_2 + A_1 = 1$$

$$-w_1 + 2w_2 + s_3 = 1$$

Step 1: Enters w_2 & leaves s_3 in initial simplex table

Step 2: Enters w_1 & leaves s_1 in first iteration ^{simplex} table

Step 3: All $z_j - c_j \geq 0$ but artificial variable appears in the basis at positive level hence dual has no optimal solⁿ.

Q.5a) ii) Graphical method procedure — 04 marks

Q.5b) i) Degeneracy Defⁿ — 2 marks
Solution — 04 marks

ii) - Defⁿ of initial basic feasible solⁿ — 02 marks
- Unbalance transportation problem — 02 marks

Q.5c) i) assignment problem as LPP — 05 marks

ii) procedure to sequencing m jobs to m machines → 05 marks.