

D. P. Coole - 5/13/66

AS3

5/13/66

①

- N.B : (1) All questions are compulsory.  
 (2) Figures to the right indicate maximum marks.  
 (3) Use of non-programmable calculators is permitted.  
 (4) Symbols used have their usual meaning

<b>Q1.</b>	<b>A)</b>	<b>Select correct answer</b>	<b>(12)</b>
	1	A body is moving in a circular orbit. Its angular momentum at a point is c) perpendicular to the plane of orbit	
	2	The time in which the amplitude of a damped harmonic oscillator decays to 1/e of its original value is called c) relaxation time	
	3	A heat engine absorbs heat at 1000 K and rejects heat at 600 K. If the engine operates at maximum possible efficiency the work done by the engine at 2000 J input is b) 1200 J	
	4	The thermal efficiency of all reversible engines working between the same two temperature limits are a) the same	
	5	A diesel engine has compression ratio from c) 15 to 20	
	6	In Joule-Thomson effect, if $\frac{2a}{RT} - b$ is positive then after expansion, the temperature a) decreases	
	<b>B)</b>	<b>Answer in one sentence</b>	<b>(03)</b>
	1	$x = C_0 e^{-2\gamma t} \sin(qt + \phi)$	
	2	Statement of property.	
	3	zero	
	<b>C)</b>	<b>Fill in the Blanks</b>	<b>(5)</b>
	1	An oscillator returns to its equilibrium state in the shortest time when it is critically damped.	
	2	Time period of a compound pendulum about centre of suspension and centre of oscillation is same or equal.	
	3	The <u>heat engine</u> is a system operating in a cyclic process that converts heat into work	
	4	If two or more engines operate between the same source but different sinks the one operating with the highest temperature difference will have the <u>highest efficiency</u> .	
	5	In Otto engine <u>air</u> is used as a working substance.	
<b>Q2.</b>	<b>A)</b>	<b>Attempt any one</b>	<b>(8)</b>
	1	Finding K.E and P.E - 2 Marks Total energy - 6 Marks	
	2	Expression for b and $\Psi$ - 2 Marks Various cases - 6 Marks	

2

	<b>B)</b>	<b>Attempt any one</b>	<b>(8)</b>
1		Definition- 2 Marks Theory – 6 Marks	
2		Derivation – 5 Marks Max and Min time period – 3 Marks	
	<b>C)</b>	<b>Attempt any one</b>	<b>(4)</b>
1		$\frac{1}{3} [(4 + 3t)\hat{i} + (5 + 6t)\hat{j} + 9\hat{k}]$	
2		Theory – 4 Marks	
<b>Q3.</b>	<b>A)</b>	<b>Attempt any one</b>	<b>(8)</b>
1		Statement of theorem – 4m Proof – 4m	
2		p – V diagram – 2m explanation of each stage – $1\frac{1}{2}$ m	
	<b>B)</b>	<b>Attempt any one</b>	<b>(8)</b>
1		Starting with the equation $TdS = C_v dT + pdV$ obtain expressions for entropy change in isothermal, isobaric and isochoric processes.	
2		Proof – 8m	
	<b>C)</b>	<b>Attempt any one</b>	<b>(4)</b>
1		Explanation – 4m	
2		$dS = \int_{T_1}^{T_2} \frac{dH}{T}$ - 1m $dH = m \times s = 10 \times 1 = 10 \text{ cal/K} - 1m$ $dS = dH \times \ln\left(\frac{T_2}{T_1}\right) - 1m$ $dS = 12.1 \text{ cal/K} - 1m$	
<b>Q4.</b>	<b>A)</b>	<b>Attempt any one</b>	<b>(8)</b>
1		Fall in temperature of the gas on expansion due to passage through the plug when initial temperature is below $T_i$ . The drop in temperature is proportional to the drop in pressure. As the initial temperature is increased upto $T_i$ , the drop in temperature becomes smaller and above $T_i$ the gas is heated up. This phenomena is Joule-Thomson effect. . . . . (2 Marks) Diagram . . . . . (2 Marks) Explanation with equations . . . . . (4 Marks)	
2		Statement : It is impossible to attain the absolute zero by any finite sequence of thermodynamic processes. . . . . (2 Marks) Consequences : Heat capacities, expansion coefficients, surface tension degeneracy of an ideal gas etc. . . . . (any two) (3 Marks each)	
	<b>B)</b>	<b>Attempt any one</b>	<b>(8)</b>

3

1	<p>Answer : Derivation of Clausius-Clapeyron equation . . . . . (4 Marks)</p> <p>If substance expands on melting, <math>dP/dT</math> is positive and therefore increase in pressure raises the melting point and vice-versa. . . . . (2 Marks)</p> <p>If substance expands on boiling, <math>dP/dT</math> is positive and therefore increase in pressure raises the boiling point and vice-versa. . . . . (2 Marks)</p>	
2	<p>p-V diagram . . . . . (3 Marks)</p> <p>Working . . . . . (5 Marks)</p>	
<b>C) Attempt any one</b>		<b>(4)</b>
1	<p>Using Maxwell's thermodynamic relation, show that for a perfect gas <math>\left(\frac{\partial U}{\partial V}\right) = 0</math></p> <p>Answer : <math>dU = dQ + pdV</math>, <math>\frac{\partial U}{\partial V} = \frac{\partial Q}{\partial V} - p</math>, <math>\frac{\partial U}{\partial V} = T\left(\frac{\partial S}{\partial V}\right) - p</math></p> <p>Maxwell' relation <math>\left(\frac{\partial S}{\partial V}\right)_T = \left(\frac{\partial P}{\partial T}\right)_V</math> <math>\frac{\partial U}{\partial V} = T\left(\frac{\partial P}{\partial T}\right) - p</math></p> <p>for perfect gas <math>pV = RT</math> <math>\frac{\partial U}{\partial V} = T\left(\frac{R}{V}\right) - p = p - p = 0</math></p>	
2	<p><math>T_l = \left(\frac{27}{4}\right) T_c</math> . . . . . (1 Mark)</p> <p>Substitution, calculation and result . . . . . (4 Marks)</p> <p><math>T_l</math> for hydrogen is <b>195.75 K</b> and for helium is <b>35.1 K</b></p>	
<b>Q5.</b>	<b>Attempt any Four</b>	<b>(20)</b>
1	<p>Definition- 2 Marks</p> <p>Derivation - 3 Marks</p>	
2	Proof - 5 Marks	
3	<p>Expression for efficiency of a Carnot engine - 1m</p> <p>Proof - 5m</p>	
4	Short Note - 5m	
5	1 Mark per point	
6	<p><math>dp = \frac{L \cdot dT}{T(v_2 - v_1)}</math> . . . . . (1 Mark)</p> <p>Substitution and calculations . . . . . (2 Marks)</p> <p><math>dP = 0.363 \text{ atm.}</math> . . . . . (1 Mark)</p> <p>Therefore required pressure = <math>1 + 0.363 = 1.363 \text{ atm.}</math> . . . . . (1 Mark)</p>	