

Q.P.: 59174

Set B

Q.1) a) i) F: prob = 0

ii) T: $P(A \cap B) = P(A) \cdot P(B)$

iii) T: $\mu_0 = E[X - E(X)]^0 = E(1) = 1$

iv) F: $V(100) = 0$

v) F: For poisson distⁿ, mean = variance one variable two outcome

Q.2) b) i) definition = 01, Example = 01

ii) Defⁿ = 01, Example = 01

iii) Defⁿ = 01, range = 01, $-1 < s < 1$

iv) $P(X) = \sum_{x=0}^y P(X=x)$ $P(Y) = \sum_{x=0}^y P(X,y)$ 01 + 01

v) (i) Poisson (ii) Binomial.

Q.3) i) I) statement + Proof + independent events = 01 + 04 + 01 \Rightarrow 06

ii) $P(\text{Accident}) = 0.0195$, $P(\text{Heavy Rain} / \text{Accident}) = 5/13$ \Rightarrow 04

iii) II) Statement + Proof = 02 + 05 = 07

IV) Req. prob = $P(A) \cdot P(\bar{B}) + P(\bar{A}) \cdot P(B) = 22/45$ 03

v) definition + Example = 01 + 01 = 2 marks each.

vi) i) 2 marks each

ii) 4 marks.

Q.4) i) I) statement + Proof + n events = 01 + 04 + 01 \Rightarrow 06

II) each 02 marks \Rightarrow 04

iii) Defⁿ = 02

iv) Def = 02 ; 5 properties = 05

v) Defⁿ = 01

vi) $\text{cov}(X,Y) = 0$, $s = 0$, X & Y are ^{NoF} independent

comment: $\text{cov}(X,Y) = 0 \nRightarrow X$ & Y are independent } 10

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- 4) I) Def: 01
II) each $V(a)$ \Rightarrow 02 , $V(ax+b)$ \Rightarrow 02 , $V(ax+bx)$ \Rightarrow 05

Q.4)

- I) Def + Ex \Rightarrow 01
2 Examples \Rightarrow 02
Mean \Rightarrow 03 Variance \Rightarrow 04

2) I) Def + $EY = 01 + 02 =$ 03

II) 02

III) $n=100$ (large) $p=0.01$ (small)

$X \sim \text{Bin}(n, p)$

$\lambda = np = 1$

$P(X=1) = e^{-1}$

05

3) Def + Mean + Variance = 01 + 04 + 05

4) I) 05 + 02

II) $p=2/5$, $n=3$ $X \sim \text{Bin}(n=3, p=2/5)$

$P(X=1) = \binom{3}{1} \left(\frac{2}{5}\right) \left(\frac{3}{5}\right)^2$

Q.5) I) Statement + Proof + n events = 01 + 02 + 01

mutually exclusive & exhaustive = 01

2) each carry 01 mark.

3) each definition 01 mark, proof = 02

4) 02 + 01 + 01 + 01

5) 05

6) Def + Mean + Variance = 01 + 03 + 01

7) Mean = 03 , $P(X=0) = e^{-3}$ = 03 + 02