

N.B. (1) Question No.1 is **compulsory**.

(2) Out of remaining **five** questions, attempt any **three** questions.

(3) Assume suitable data, if required but justify the same.

(4) Figures to the right indicate full marks.

(5) Use of **Statistical Table** is allowed.

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|---|----|--|------|
| 1 | a) | Discuss Properties a pseudo random numbers generator should fulfill. | (5) |
| | b) | Explain One channel and two channel Queuing model with an example. | (5) |
| | c) | Show that exponential distribution is memory less. | (5) |
| | d) | Explain process of model building. | (5) |
| 2 | a) | Explain how to select family of distribution when historical data is available. | (10) |
| | b) | Conduct chi-sq test for the given set of pseudo random numbers. Clearly state your conclusion. | |

| | | | | | | | | | |
|------|------|------|------|------|------|------|------|------|------|
| 0.40 | 0.74 | 0.32 | 0.63 | 0.94 | 0.51 | 0.62 | 0.41 | 0.17 | 0.66 |
| 0.98 | 0.44 | 0.20 | 0.87 | 0.62 | 0.27 | 0.25 | 0.78 | 0.93 | 0.39 |
| 0.42 | 0.60 | 0.25 | 0.43 | 0.11 | 0.44 | 0.59 | 0.73 | 0.97 | 0.88 |
| 1.00 | 0.59 | 0.56 | 0.89 | 0.57 | 0.87 | 0.30 | 0.52 | 0.09 | 0.42 |
| 0.43 | 0.35 | 0.44 | 0.28 | 0.57 | 0.23 | 0.53 | 0.75 | 0.15 | 0.07 |
| 0.97 | 0.65 | 0.35 | 0.41 | 0.11 | 0.08 | 0.97 | 0.55 | 0.93 | 0.33 |
| 0.82 | 0.63 | 0.52 | 0.21 | 0.71 | 0.60 | 0.39 | 0.14 | 0.57 | 0.06 |
| 0.82 | 0.48 | 0.66 | 0.34 | 0.81 | 0.73 | 0.90 | 0.26 | 0.38 | 0.58 |
| 0.50 | 0.61 | 0.80 | 0.56 | 0.08 | 0.80 | 0.37 | 0.56 | 0.02 | 0.46 |
| 0.13 | 0.36 | 0.17 | 0.67 | 0.93 | 0.25 | 0.18 | 0.25 | 0.86 | 0.83 |

Assume Critical Value to be $\lambda^2_{(0.05,9)} = 16.9$.

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|---|----|---|------|
| 3 | a) | Explain any one method of generating pseudo random numbers. Explain the term "period" in the context of random number generators. | (10) |
| | b) | Conduct KS test on the following random numbers and give your conclusion | |

| | | | | |
|------|------|------|------|------|
| 0.44 | 0.76 | 0.21 | 0.45 | 0.16 |
|------|------|------|------|------|

(10)

Assume critical value $D_c = 0.565$.

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|---|----|--|------|
| 4 | a) | Generate random variate for exponential and Uniform distribution | (10) |
| | b) | Conduct run above and below mean test for the given random numbers | |

| | | | | | | | | | |
|------|------|------|------|------|------|------|------|------|------|
| 0.76 | 0.57 | 0.52 | 0.05 | 0.92 | 0.86 | 0.95 | 0.36 | 0.46 | 0.65 |
| 0.63 | 0.81 | 0.98 | 0.85 | 0.42 | 0.82 | 0.55 | 0.90 | 0.13 | 0.93 |
| 0.85 | 0.46 | 0.36 | 0.63 | 0.70 | 0.41 | 0.12 | 0.61 | 0.24 | 0.12 |
| 0.85 | 0.01 | 0.43 | 0.27 | 0.94 | 0.61 | 0.62 | 0.45 | 0.71 | 0.19 |
| 0.96 | 0.89 | 0.18 | 0.45 | 0.17 | 0.35 | 0.46 | 0.70 | 0.43 | 0.73 |

(10)

Assume critical value $Z_c = 1.96$.

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- 5 a) Explain widely used steps for calibration and validation of models (10)
 b) Given single channel queuing model has following characteristics. Find efficiency, average wait time and probability of wait.

| Probability | Time b/w Arrival | Probability | Service time |
|-------------|------------------|-------------|--------------|
| 0.20 | 1 | 0.20 | 1 |
| 0.10 | 3 | 0.15 | 2 |
| 0.25 | 4 | 0.25 | 3 |
| 0.30 | 2 | 0.30 | 4 |
| 0.15 | 6 | 0.1 | 5 |

- 6 a) Explain the concept of point estimator and interval estimator with respect to terminating simulation. (10)
 b) Discuss areas of application of simulation and modeling. (10)

Random Number Table

| | | | | | | | | | |
|------|------|------|------|------|------|------|------|------|------|
| 0.51 | 0.20 | 0.08 | 0.04 | 0.19 | 0.21 | 0.48 | 0.80 | 0.86 | 0.65 |
| 0.65 | 0.50 | 0.91 | 0.77 | 0.47 | 0.68 | 0.75 | 0.34 | 0.70 | 0.80 |
| 0.52 | 0.62 | 0.92 | 0.26 | 0.59 | 0.35 | 0.07 | 0.58 | 0.33 | 0.66 |
| 0.40 | 0.26 | 0.80 | 0.56 | 0.10 | 0.41 | 0.51 | 0.14 | 0.05 | 0.29 |
| 0.64 | 0.31 | 0.43 | 0.95 | 0.71 | 0.31 | 0.38 | 0.48 | 0.25 | 0.37 |
| 0.64 | 0.94 | 0.97 | 0.62 | 0.97 | 0.09 | 0.03 | 0.77 | 0.80 | 0.29 |
| 0.09 | 0.23 | 0.70 | 0.78 | 0.73 | 0.78 | 0.29 | 0.44 | 0.24 | 0.43 |
| 0.80 | 0.07 | 0.41 | 0.46 | 0.70 | 0.50 | 0.60 | 0.59 | 0.98 | 0.28 |
| 0.12 | 0.76 | 0.59 | 0.94 | 0.76 | 0.24 | 0.12 | 0.87 | 0.25 | 0.02 |
| 0.99 | 0.73 | 0.37 | 0.06 | 0.63 | 0.23 | 0.87 | 0.51 | 0.05 | 0.89 |
| 0.69 | 0.31 | 0.45 | 0.28 | 0.37 | 0.86 | 0.01 | 0.47 | 0.81 | 0.18 |
| 0.78 | 0.72 | 0.81 | 0.56 | 0.71 | 0.35 | 0.44 | 0.63 | 0.77 | 0.32 |
| 0.80 | 0.83 | 0.47 | 0.20 | 0.58 | 0.21 | 1.00 | 0.34 | 0.36 | 0.42 |
| 0.81 | 0.05 | 0.10 | 0.74 | 0.88 | 0.90 | 0.04 | 0.17 | 0.00 | 0.16 |
| 0.96 | 0.26 | 0.88 | 0.51 | 0.60 | 0.72 | 0.75 | 0.91 | 0.43 | 0.17 |
| 0.05 | 0.56 | 0.31 | 0.35 | 0.65 | 0.62 | 0.25 | 0.24 | 0.41 | 0.89 |
| 0.14 | 0.57 | 0.05 | 0.48 | 0.43 | 0.69 | 0.01 | 0.53 | 0.55 | 0.11 |
| 0.41 | 0.18 | 0.72 | 0.18 | 0.00 | 0.13 | 0.62 | 0.49 | 0.77 | 0.42 |
| 0.61 | 0.03 | 0.61 | 0.97 | 0.39 | 0.89 | 0.29 | 0.27 | 0.20 | 0.93 |
| 0.56 | 0.24 | 0.33 | 0.01 | 0.62 | 0.39 | 0.59 | 0.63 | 0.06 | 0.98 |
